

Kerr black holes with scalar (or Proca) hair

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Gravitational lensing of the Aveiro Campus by a Kerr black hole with scalar hair

IAU Symposium 324 “New Frontiers in Black Hole Astrophysics”, Ljubljana, Slovenia
September 15th 2016

based on

[PRL112\(2014\)221101](#)

[CQG32\(2015\)144001](#)

[PRL115\(2015\)211102](#)

with E. Radu, P. Cunha, H. Rúnarsson

Take-home message:

It is common lore that,
in Einstein's gravity,
with reasonable matter sources
of Astrophysical interest...

**...Black Holes cannot have hair
(for instance, simple scalar "hair")**

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**...Black Holes cannot have hair
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**They actually can,
if massive, complex, scalar fields exist.**

Take-home message:

In Einstein's gravity minimally coupled to a massive, complex, scalar field there are BH solutions:

- **within GR** (not alternative theories of gravity);
- with matter **obeying all energy conditions**;

which are:

- asymptotically flat
 - regular on and outside the horizon
 - continuously connecting to the Kerr solution
 - continuously connected to relativistic Bose-Einstein condensates (boson stars)
 - with an independent scalar "charge" (primary hair)
- which can yield **distinct phenomenology**;

Kerr Black Holes with scalar hair

C.H. and Radu, Phys. Rev. Lett. 112 (2014) 221101

2) Why?

Linear analysis: Klein-Gordon equation in Kerr

$$\square\Phi = \mu^2\Phi$$

$$\Phi = e^{-i\omega t} e^{im\varphi} S_{\ell m}(\theta) R_{\ell m}(r)$$

Radial Teukolsky equation: Teukolsky (1972); Brill et al. (1972)

$$\frac{d}{dr} \left(\Delta \frac{dR_{\ell m}}{dr} \right) = \left(a^2 \omega^2 - 2maw + \mu^2 r^2 + A_{\ell m} - \frac{K^2}{\Delta} \right) R_{\ell m}$$

$$\Delta \equiv r^2 - 2Mr + a^2$$

$$K \equiv (r^2 + a^2)\omega - am$$

Generically one obtains *quasi*-bound states:

$$\omega = \omega_R + i\omega_I$$

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$$\omega_I < 0 \quad \text{if} \quad \omega_R > \omega_c \quad \text{decay}$$

critical frequency

$$\omega = \omega_R + i\omega_I$$

$$\omega_c = m\Omega_H$$

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grow

Press and Teukolsky
(1972)

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$$\omega_c = m\Omega_H$$

$$\omega = \omega_R + i\omega_I$$

$$\omega_I = 0 \quad \text{if} \quad \omega = \omega_c$$

true bound states:

stationary clouds

Hod (2012)

$$\omega_I > 0 \quad \text{if} \quad \omega_R < \omega_c$$

grow

Press and Teukolsky
(1972)

**Backreacting clouds
yield**

Kerr black holes with scalar hair

Einstein Klein-Gordon: non-linear setup

Ansatz:

$$ds^2 = -e^{2F_0(r,\theta)} N dt^2 + e^{2F_1(r,\theta)} \left(\frac{dr^2}{N} + r^2 d\theta^2 \right) + e^{2F_2(r,\theta)} r^2 \sin^2 \theta (d\varphi - W(r,\theta) dt)^2 \quad N = 1 - \frac{r_H}{r}$$
$$\Phi = \phi(r, \theta) e^{i(m\varphi - wt)} \quad w = m\Omega_H$$

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“non-metric-symmetry inheritance” by matter field,
circumvents generic no-scalar hair theorems

Einstein Klein-Gordon: non-linear setup

Ansatz:

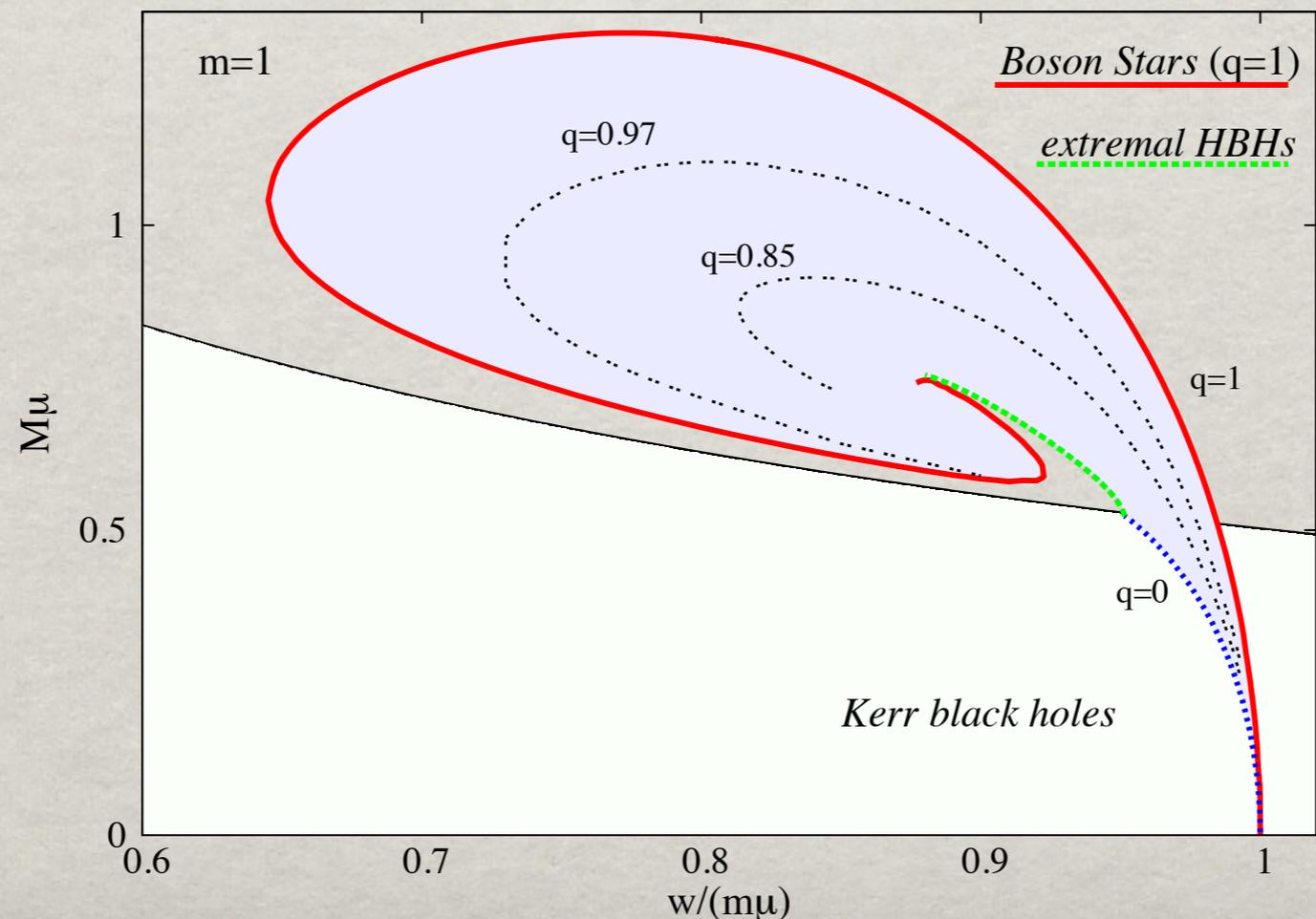
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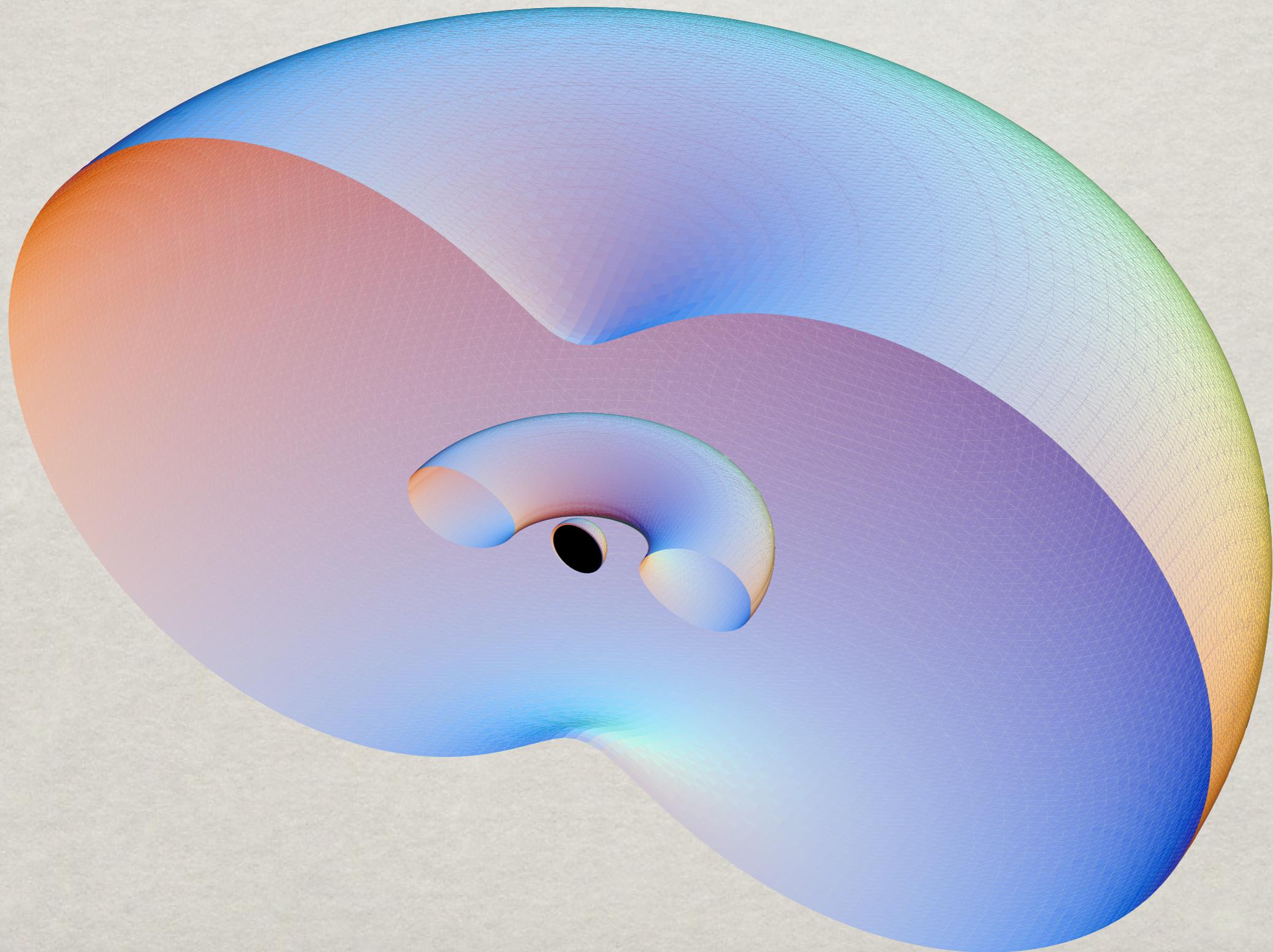
$$w = m\Omega_H$$

Space of solutions



Kerr BHs with scalar hair

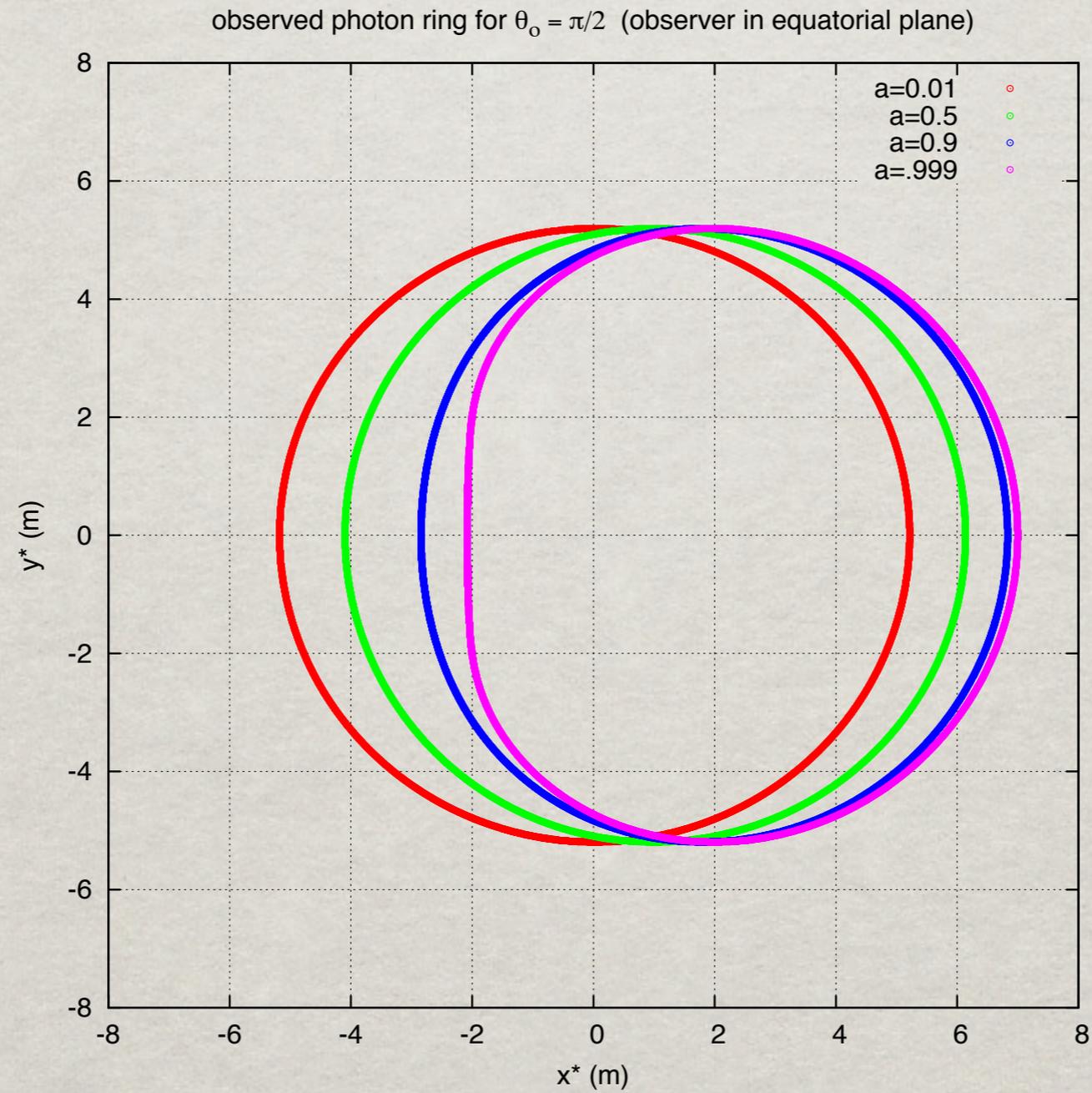
Numerical data: <http://gravitation.web.ua.pt/>



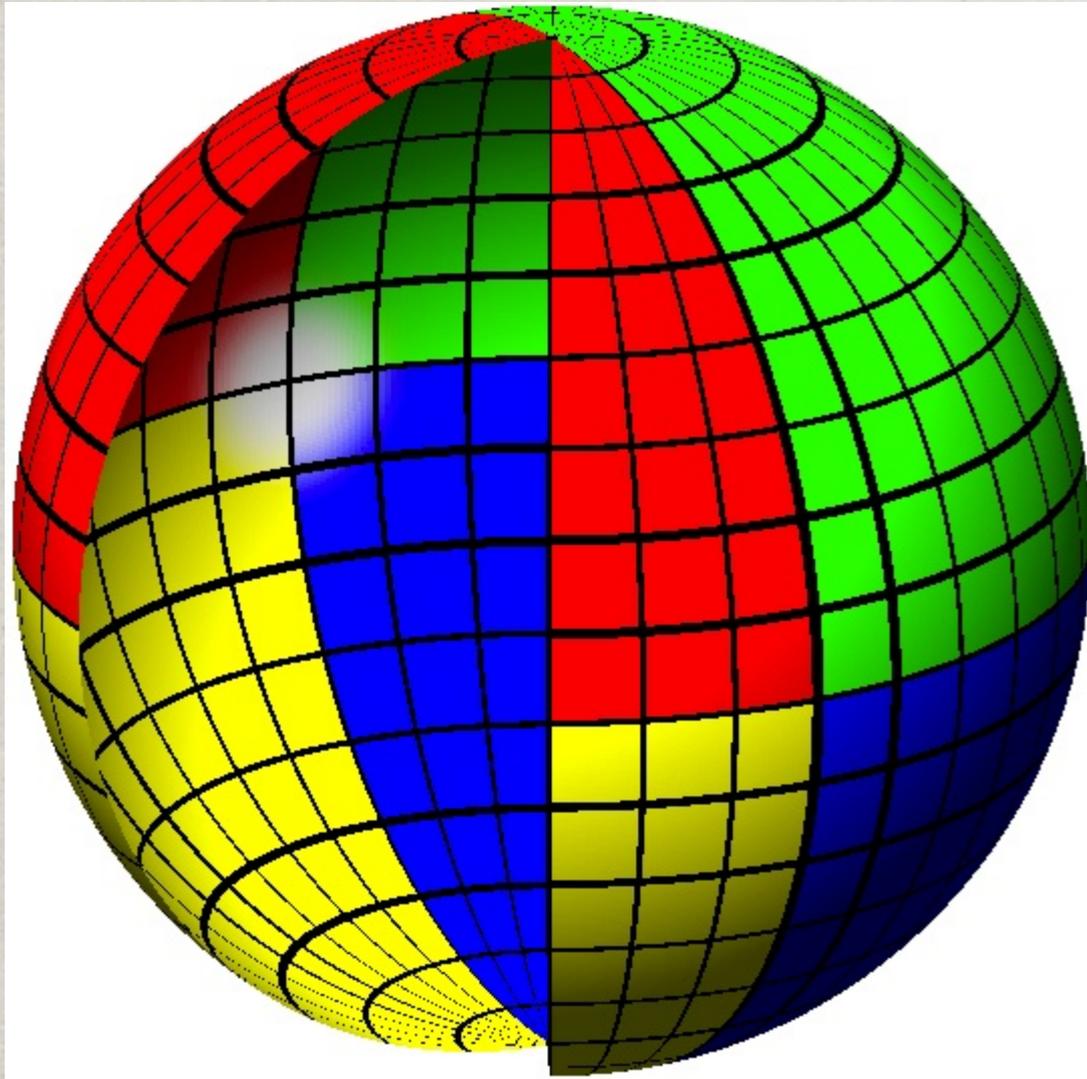
3) Could we distinguish them in the sky?

The shadow of a black hole:

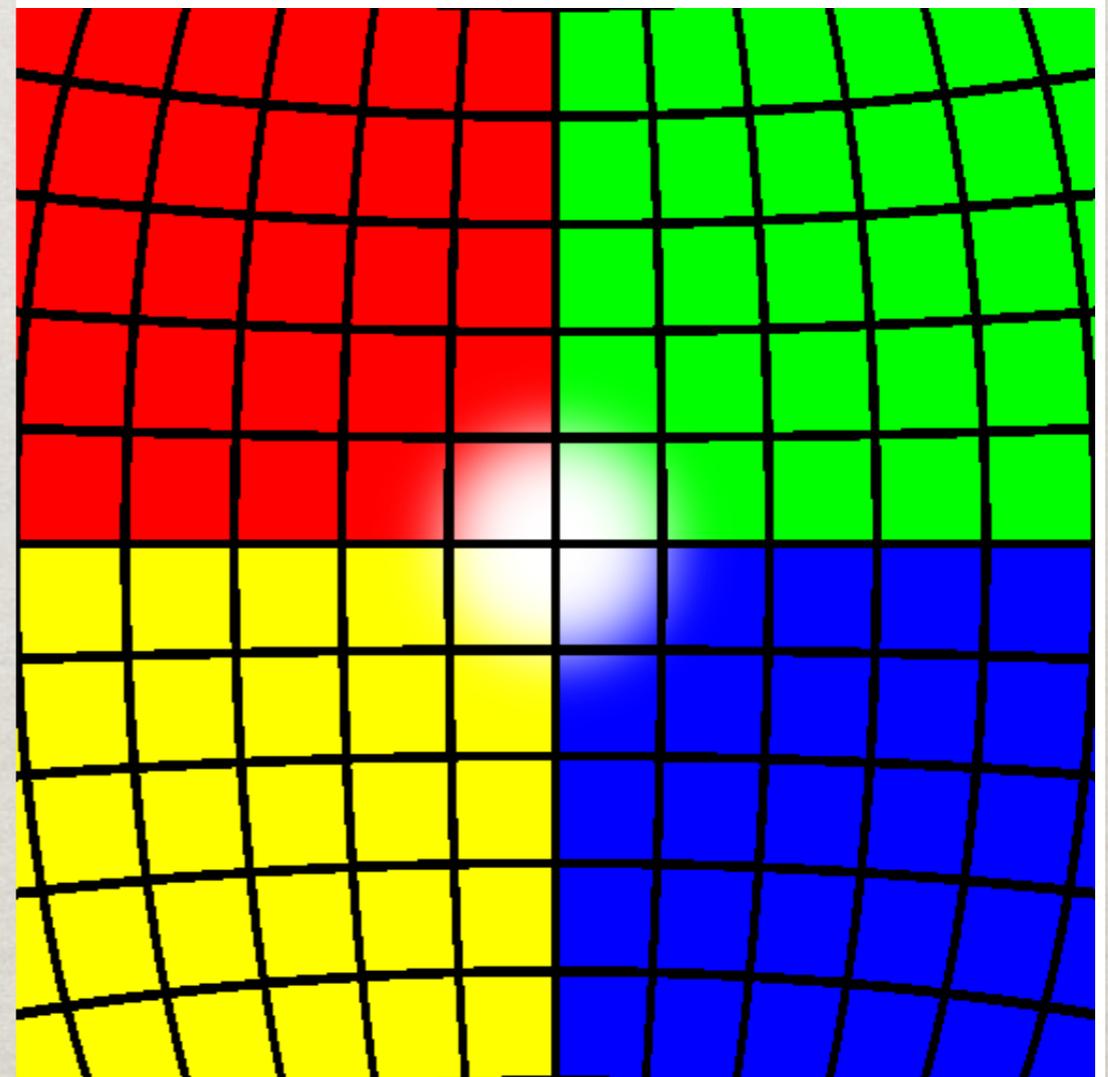
Kerr



We have performed ray tracing to compute lensing and shadows.

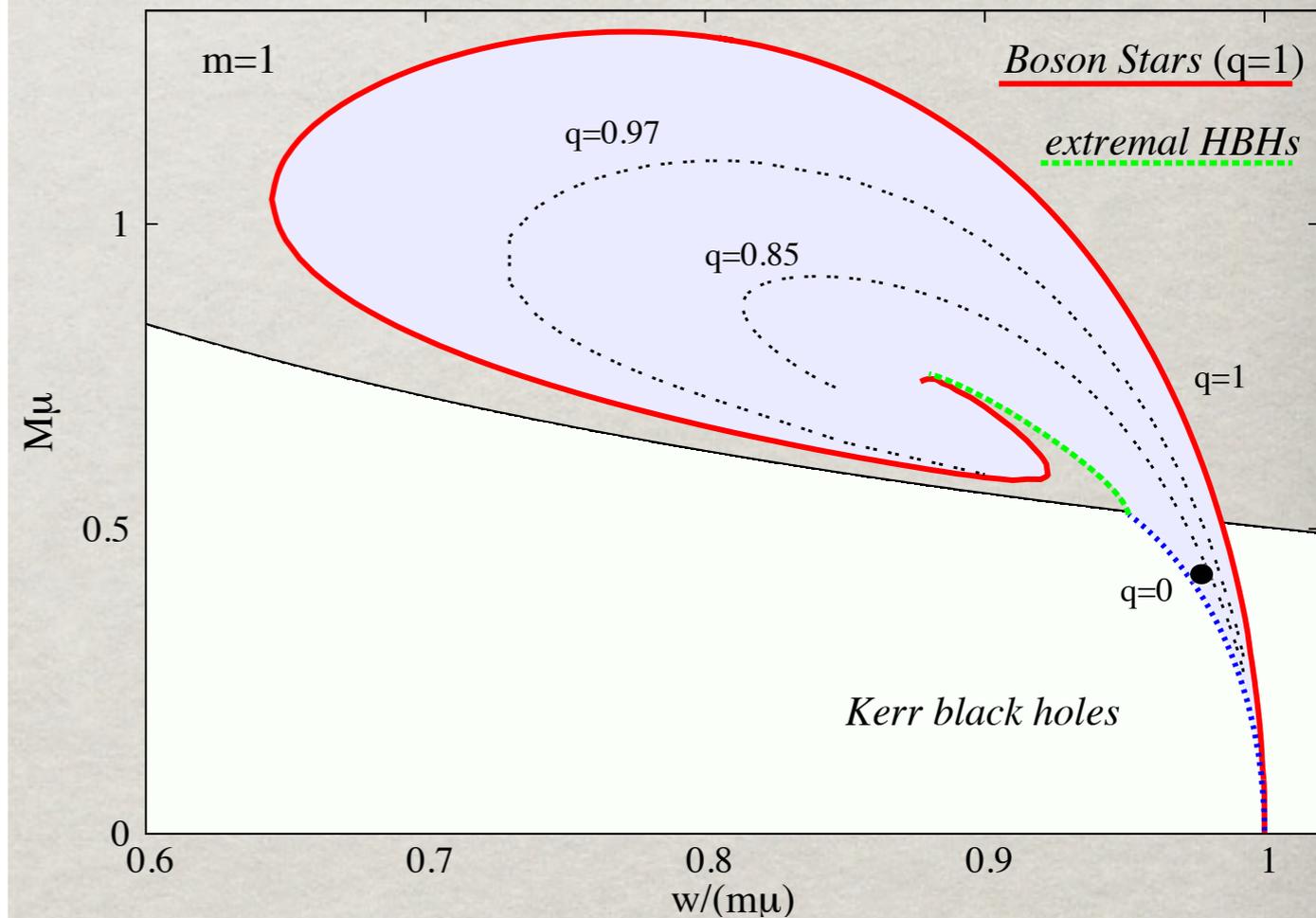
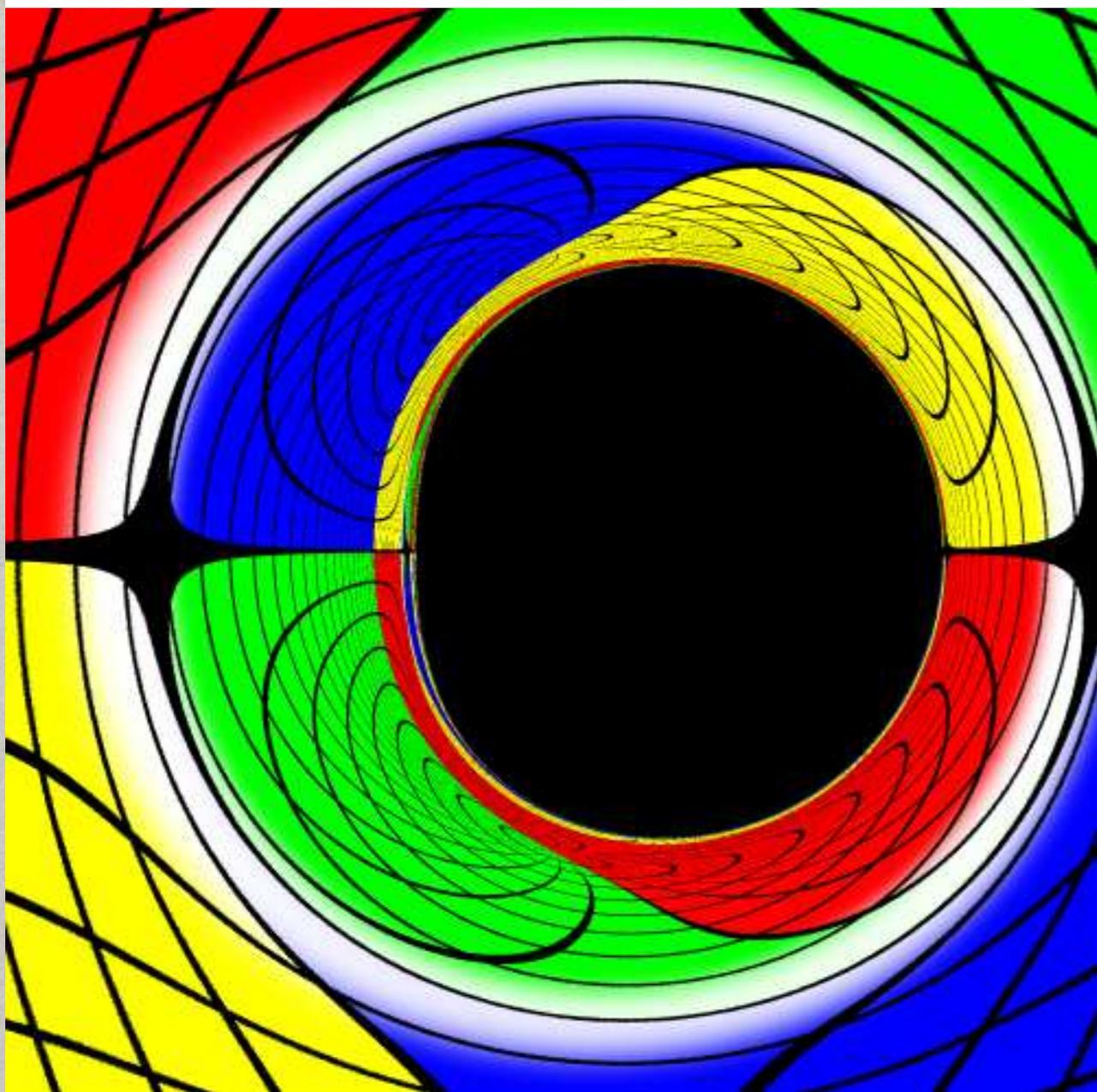


The full celestial sphere



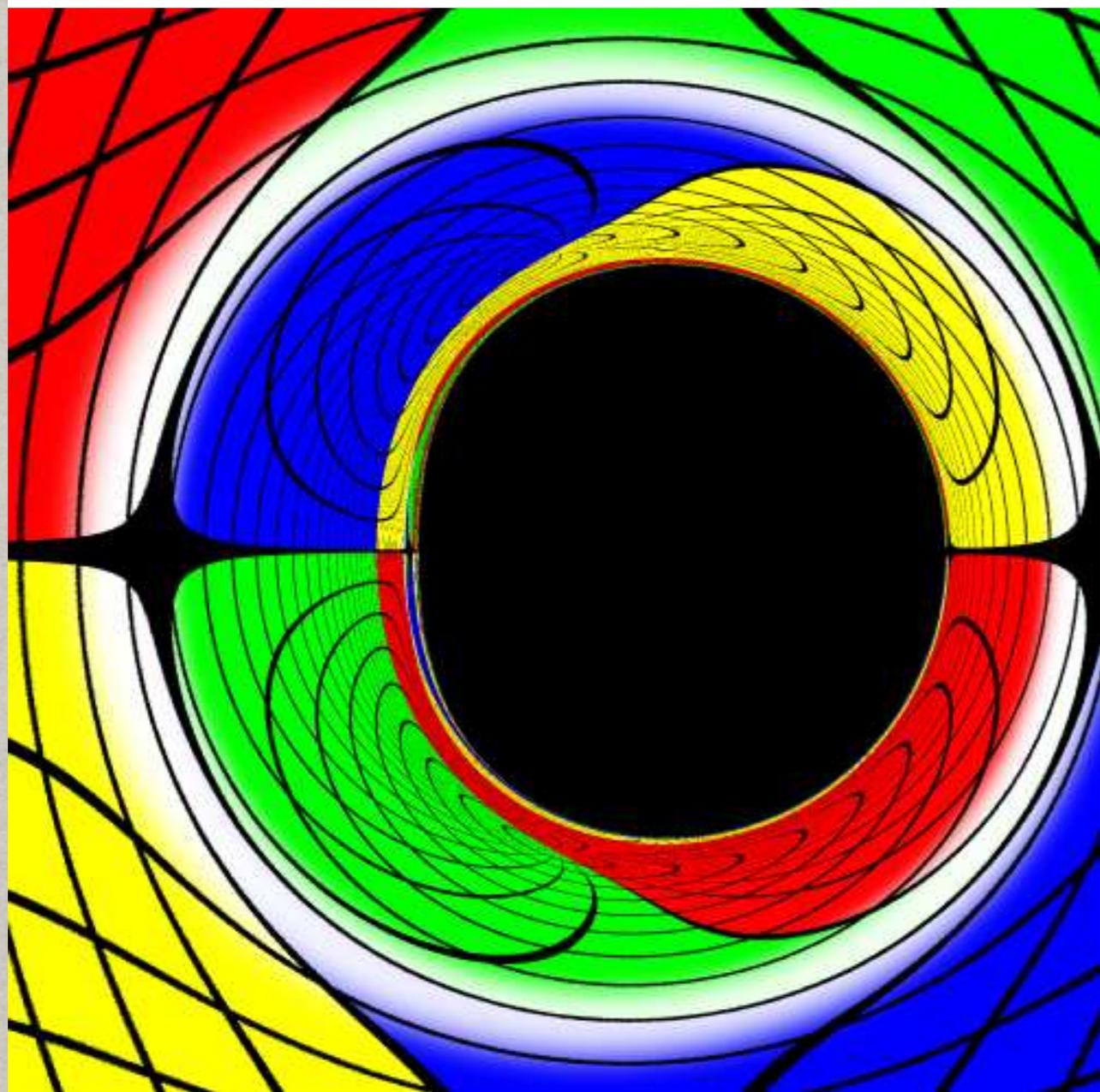
The “camera” opening angle

A Kerr-like hairy black hole

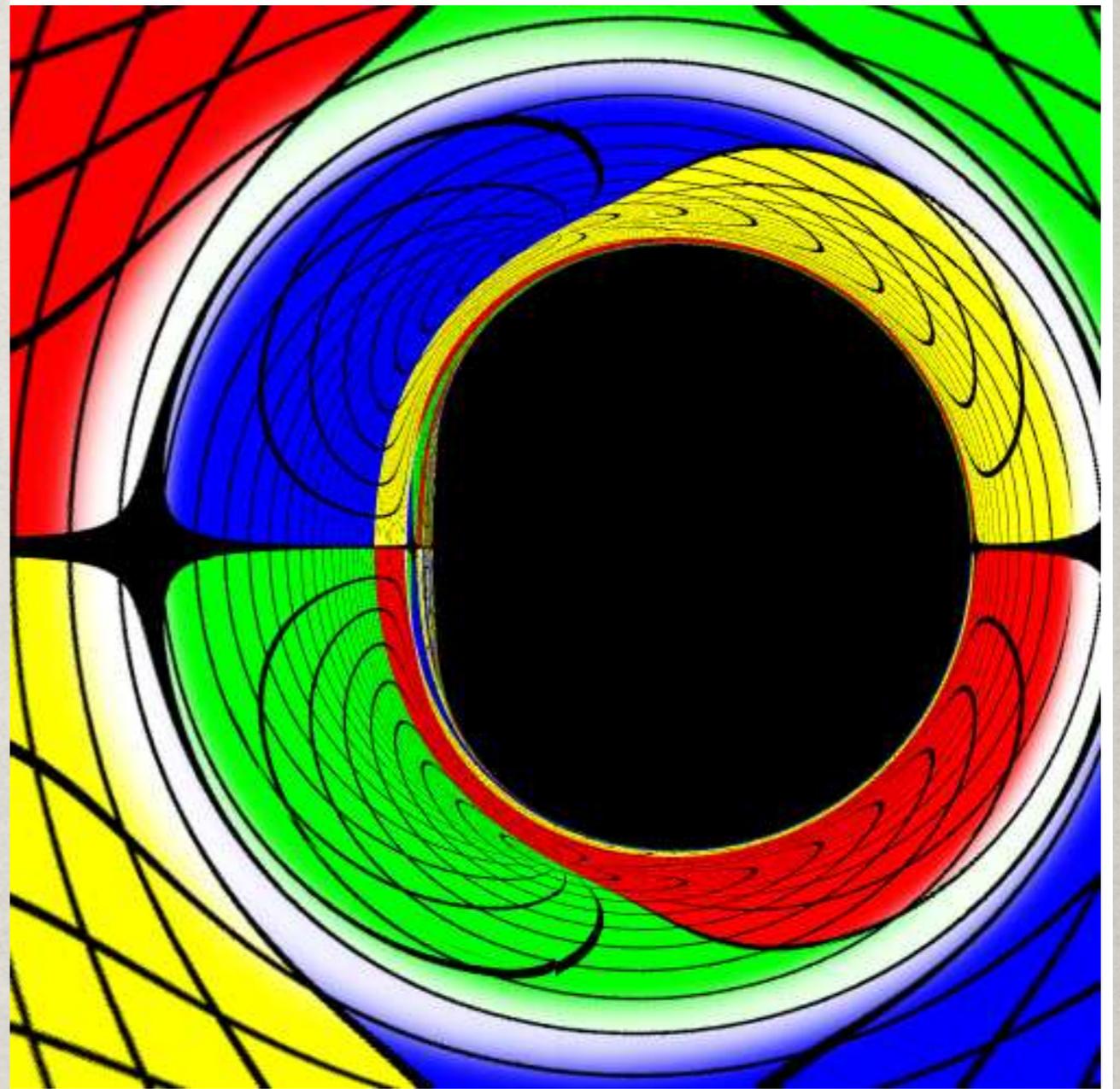


5% of mass;
13% of angular momentum
is stored in the scalar field

A Kerr-like Kerr BH with scalar hair

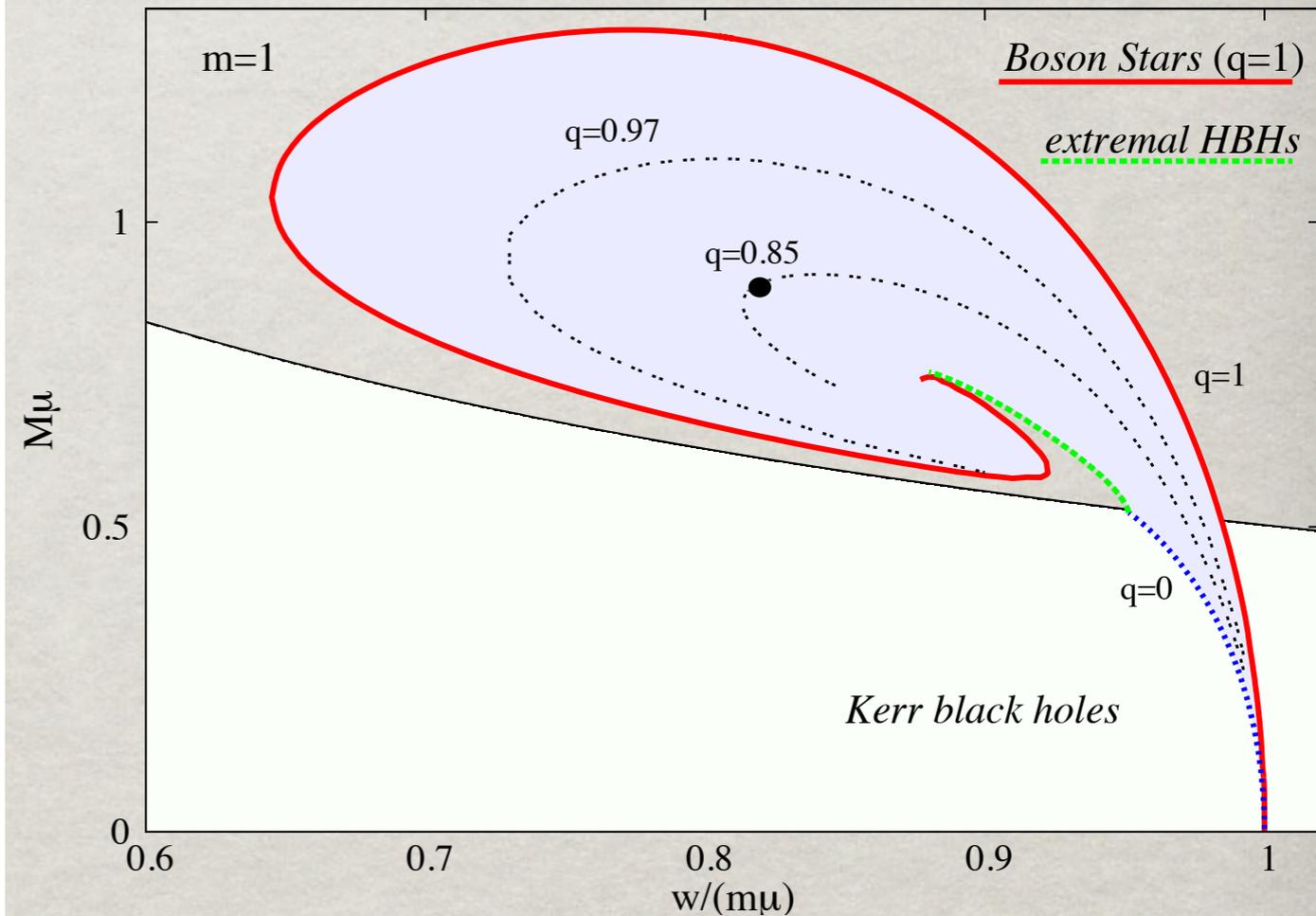
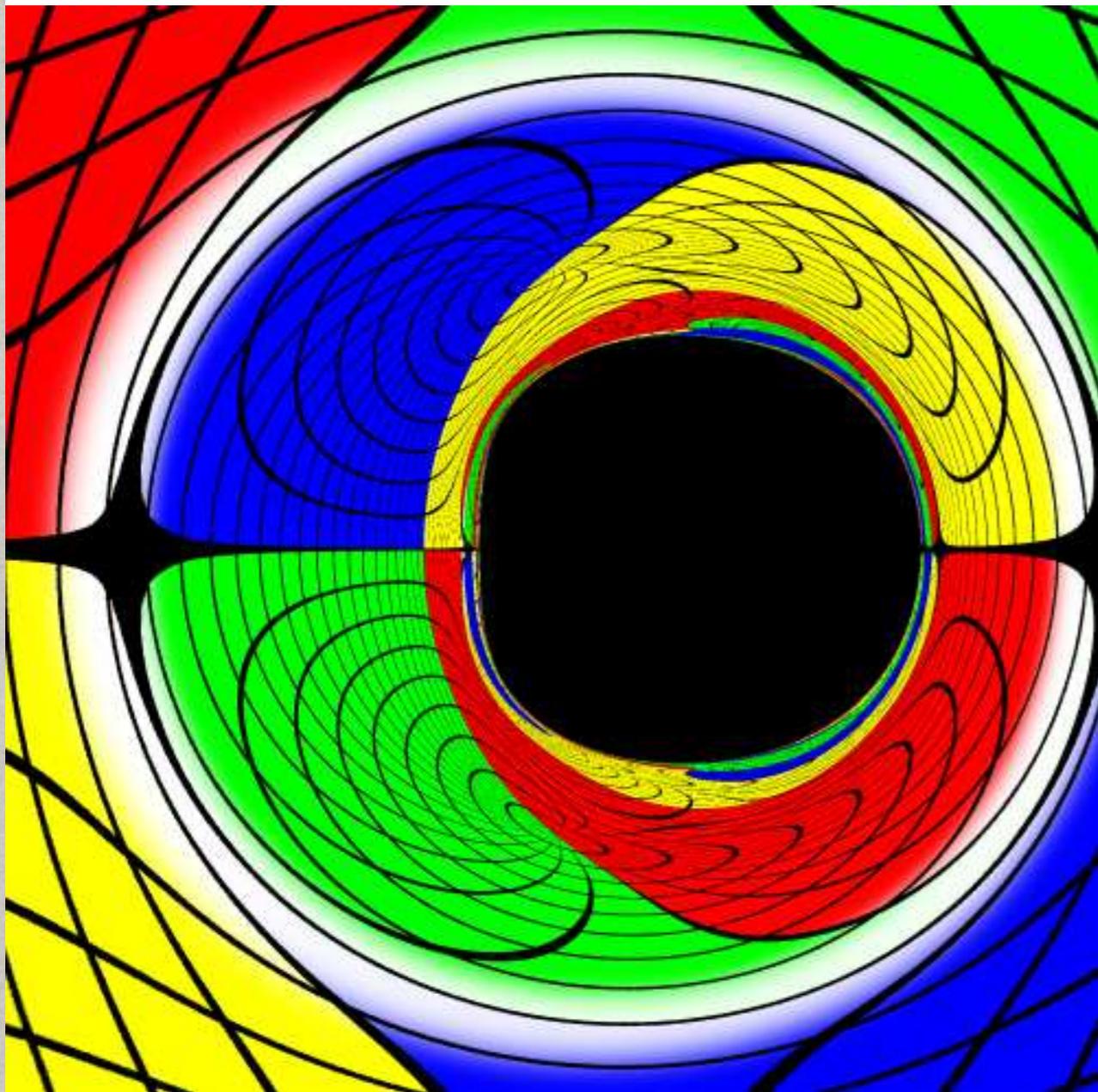


Kerr BH with scalar hair
 $M=0.393$; $J=0.15$ (horizon)
 $M=0.022$; $J=0.022$ (scalar field)



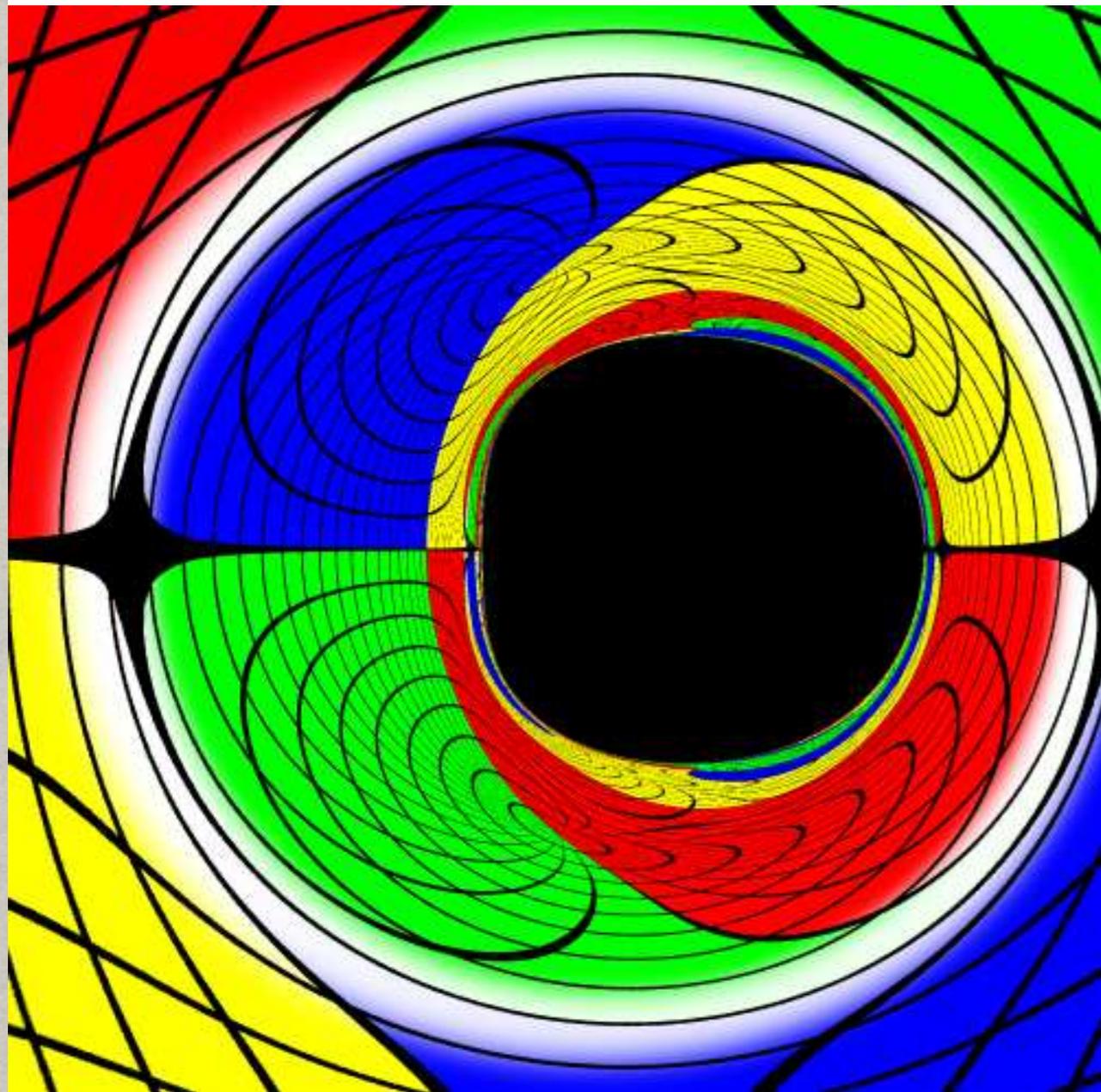
Vacuum Kerr BH
 $M=0.415$; $J=0.172$

A non-Kerr-like hairy black hole

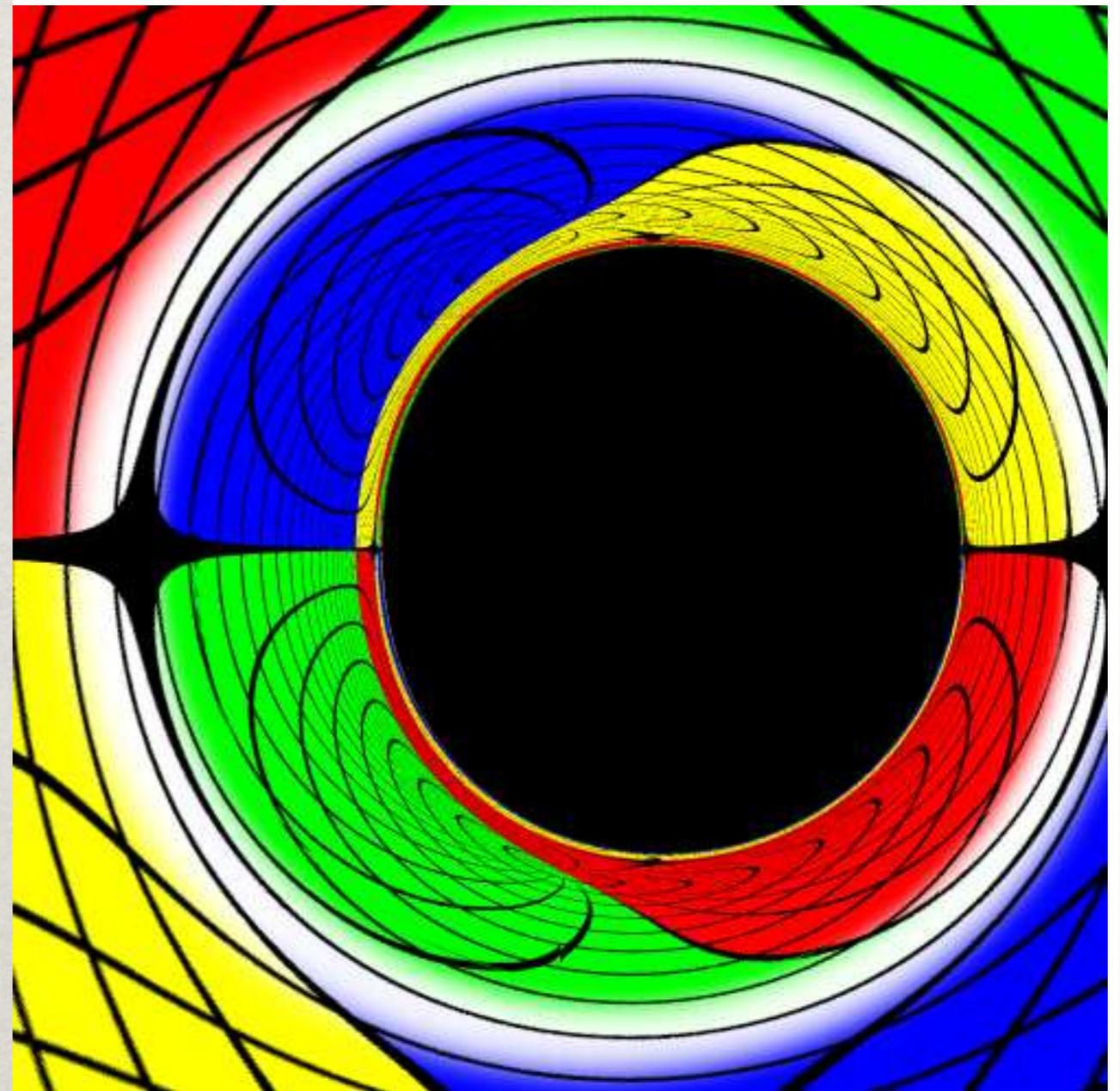


75% of mass;
85% of angular momentum
is stored in the scalar field

A non-Kerr-like hairy black hole

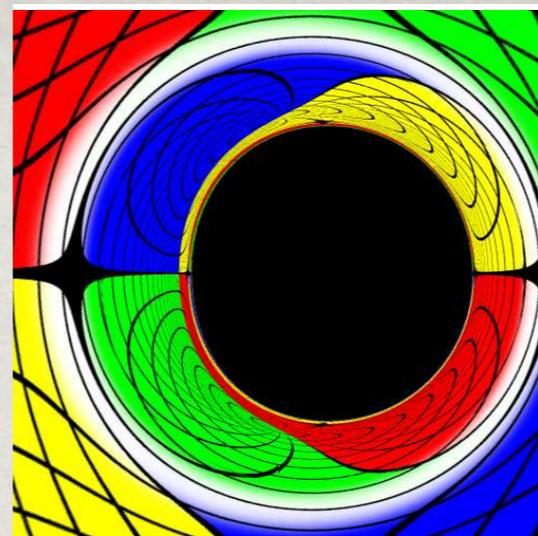
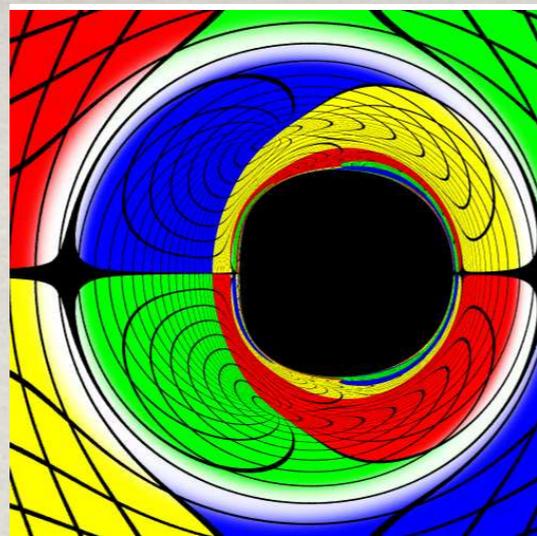


Kerr BH with scalar hair
 $M=0.234$; $J=0.114$ (horizon)
 $M=0.699$; $J=0.625$ (scalar field)

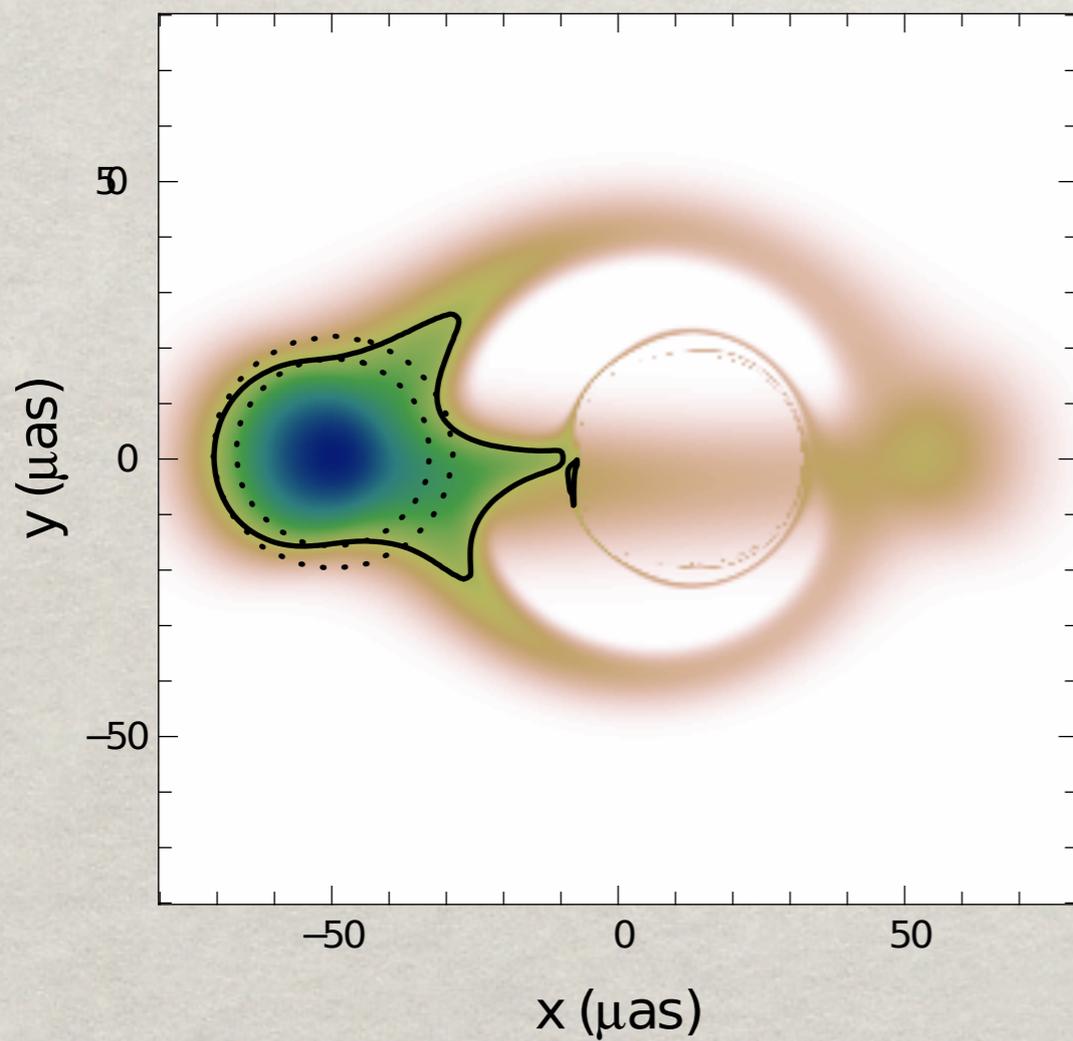


Vacuum Kerr BH
 $M=0.933$; $J=0.739$

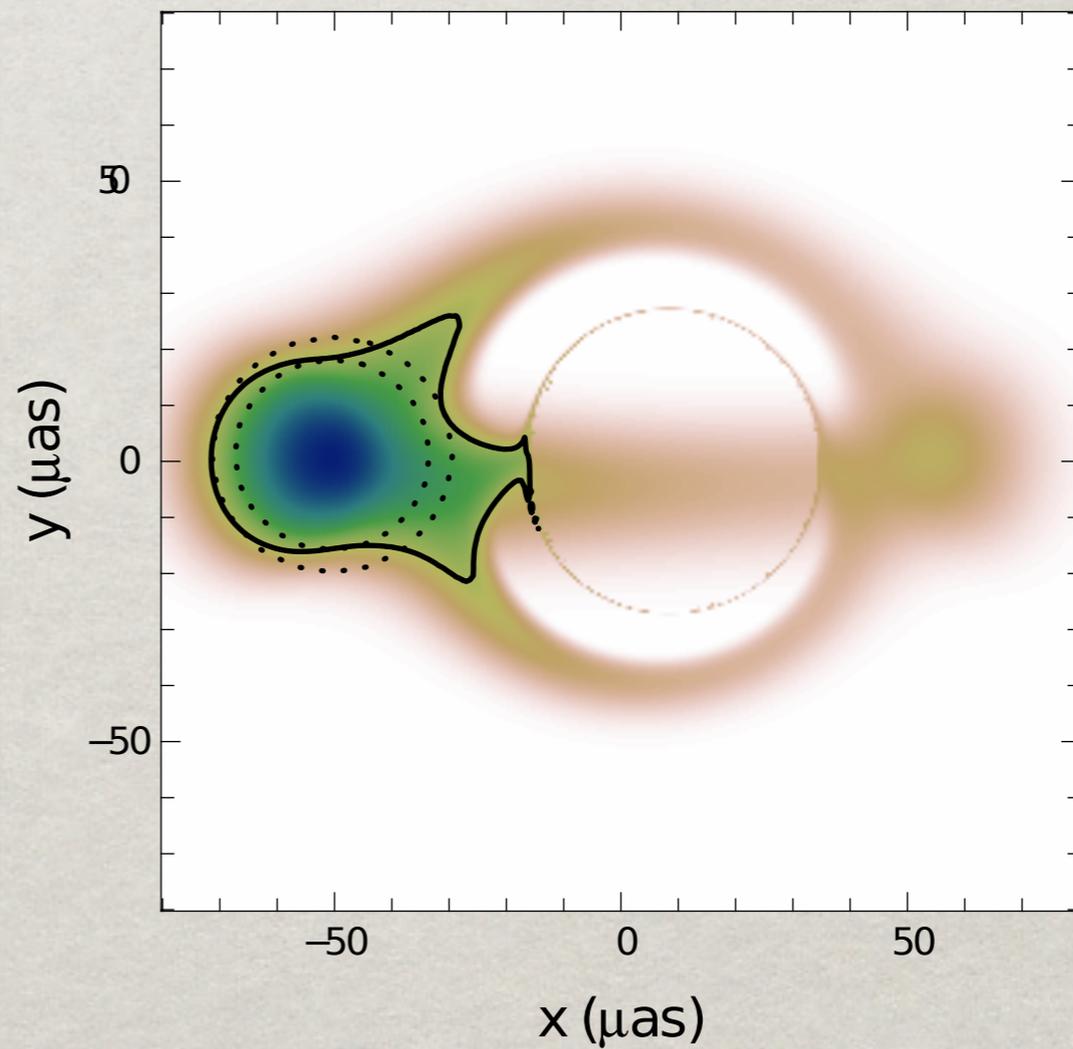
“Academic
Setup”



KBHSH configuration II



Kerr SP configuration II



Differences remain in an astrophysically more realistic setup

Vincent, Gourgoulhon, C.H., Radu, arXiv:160604246

4) Not one family of solutions... rather, one mechanism

A (hairless) BH which is afflicted by the superradiant instability of a given field for which the energy-momentum tensor is time-independent, allows a hairy generalization with that field.

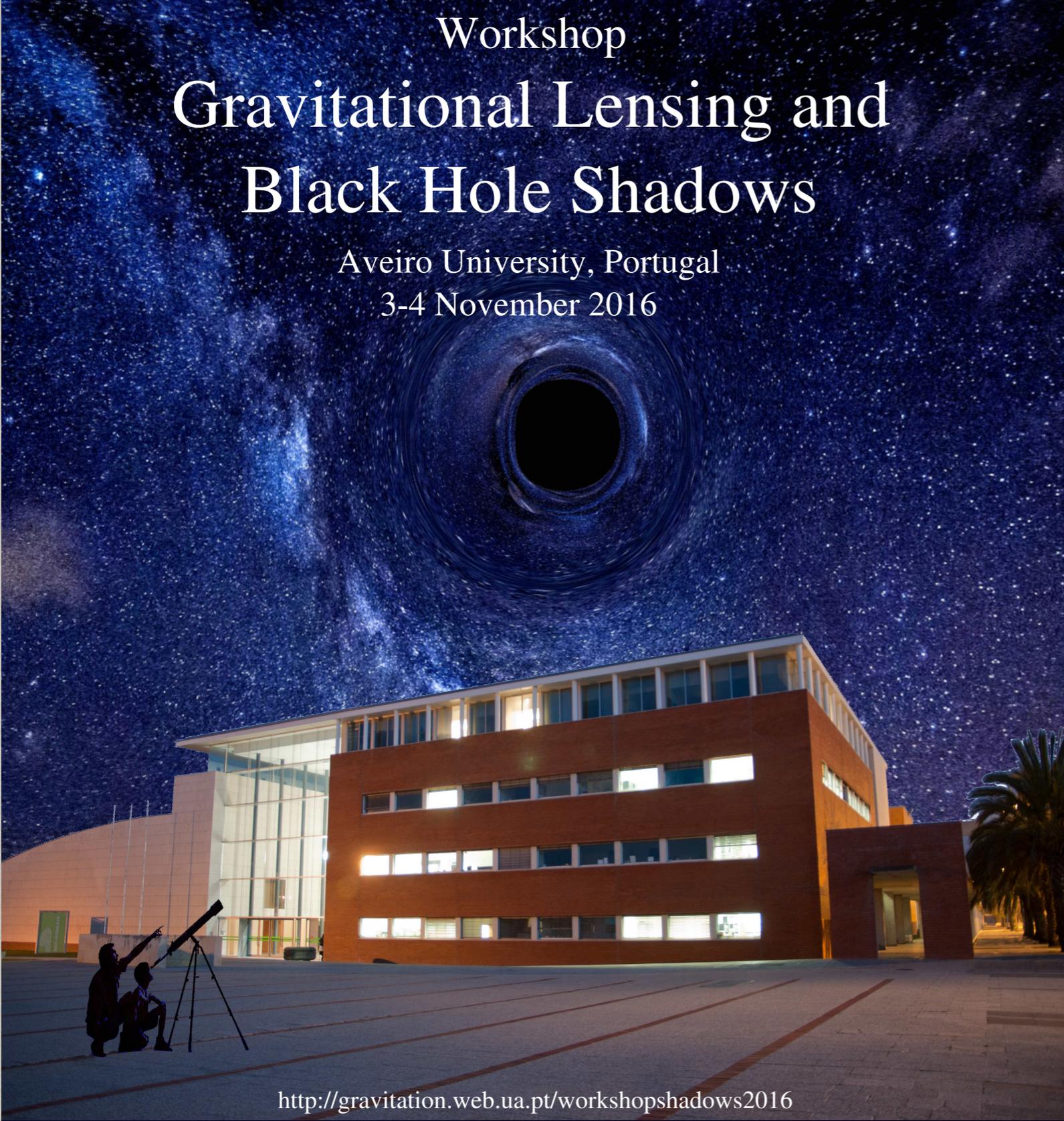
C. H., E. Radu, IJMPD23(2014)1442014

e.g. Kerr black holes with Proca hair have been constructed:

C.H., Radu and Rúnarsson,
CQG33(2016)154001

Conclusions:

- Timely to study alternatives to the Kerr paradigm, in view of all the ongoing and upcoming observations (electromagnetic and GWs)
- There is a new, physically reasonable model of black holes, within GR, which can be used to make contact with fundamental high energy physics
- Many open questions about the properties of these solutions, in particular about their dynamics, e.g. likelihood of formation and stability.



Workshop
Gravitational Lensing and
Black Hole Shadows

Aveiro University, Portugal
3-4 November 2016

<http://gravitation.web.ua.pt/workshopshadows2016>

Mini Courses:

| Jai Grover & Alex Wittig (ESA): Pyhole and GPU powered raytracing in Python
| Frederic Vincent (Observatoire de Paris): GYOTO

Organisers:

| V. Cardoso | P. Cunha | C. Herdeiro | J. S. Lemos | E. Radu | H. Rúnarsson |

Thank you for your
attention!

5) Could they form dynamically?

Question:

In these models
vacuum Kerr black holes are **unstable**
(against superradiance).

What is the endpoint of the instability?

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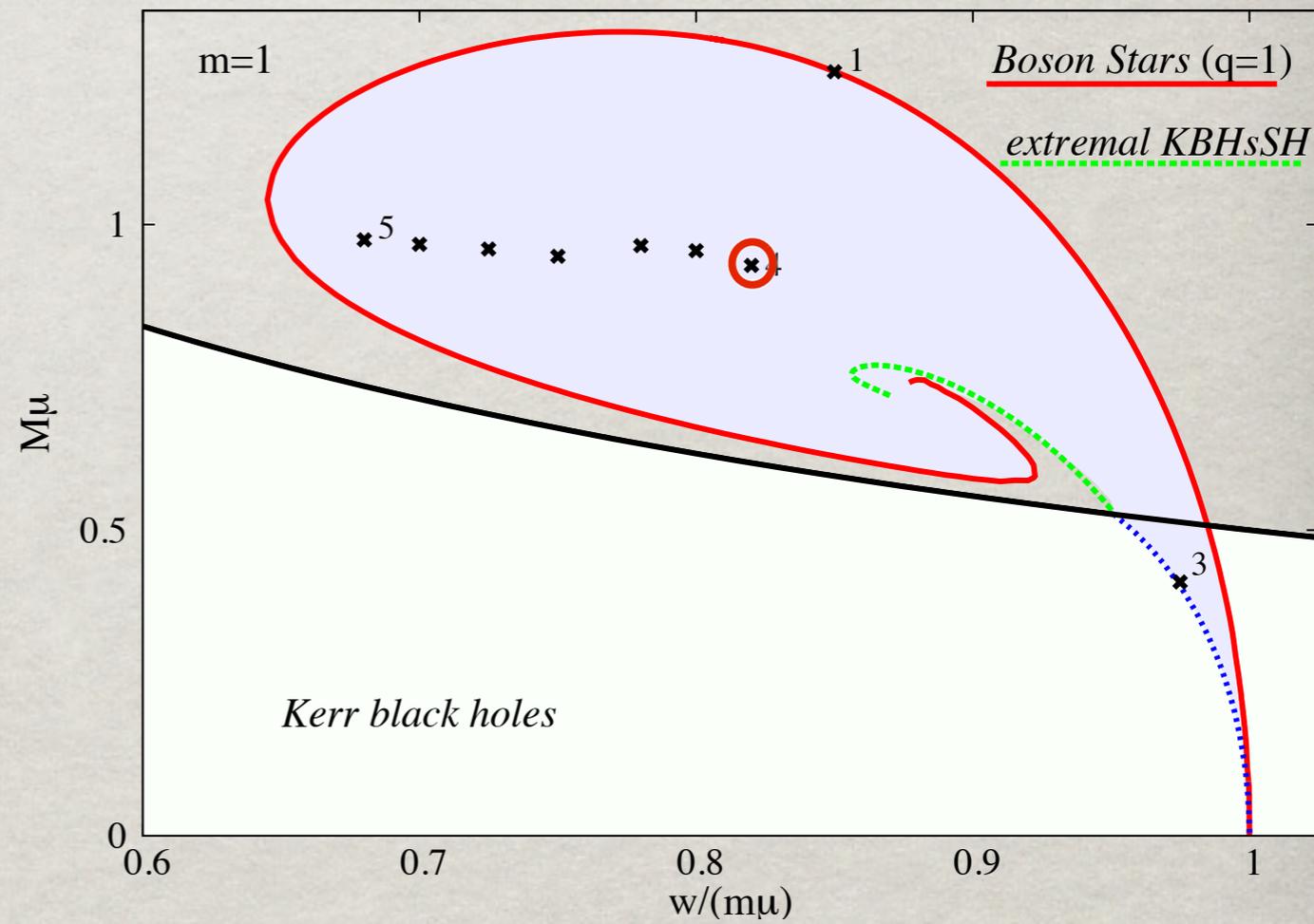
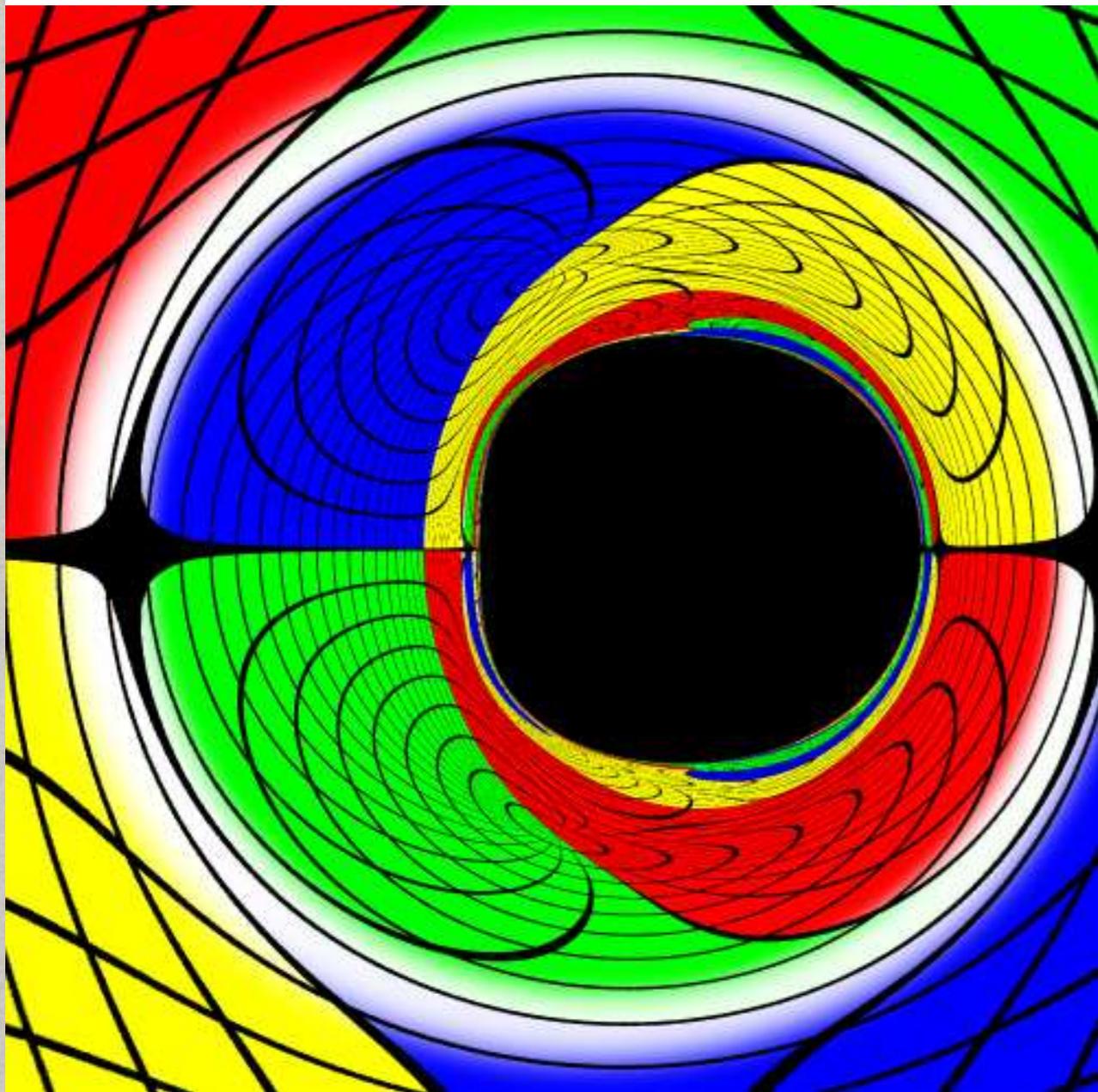
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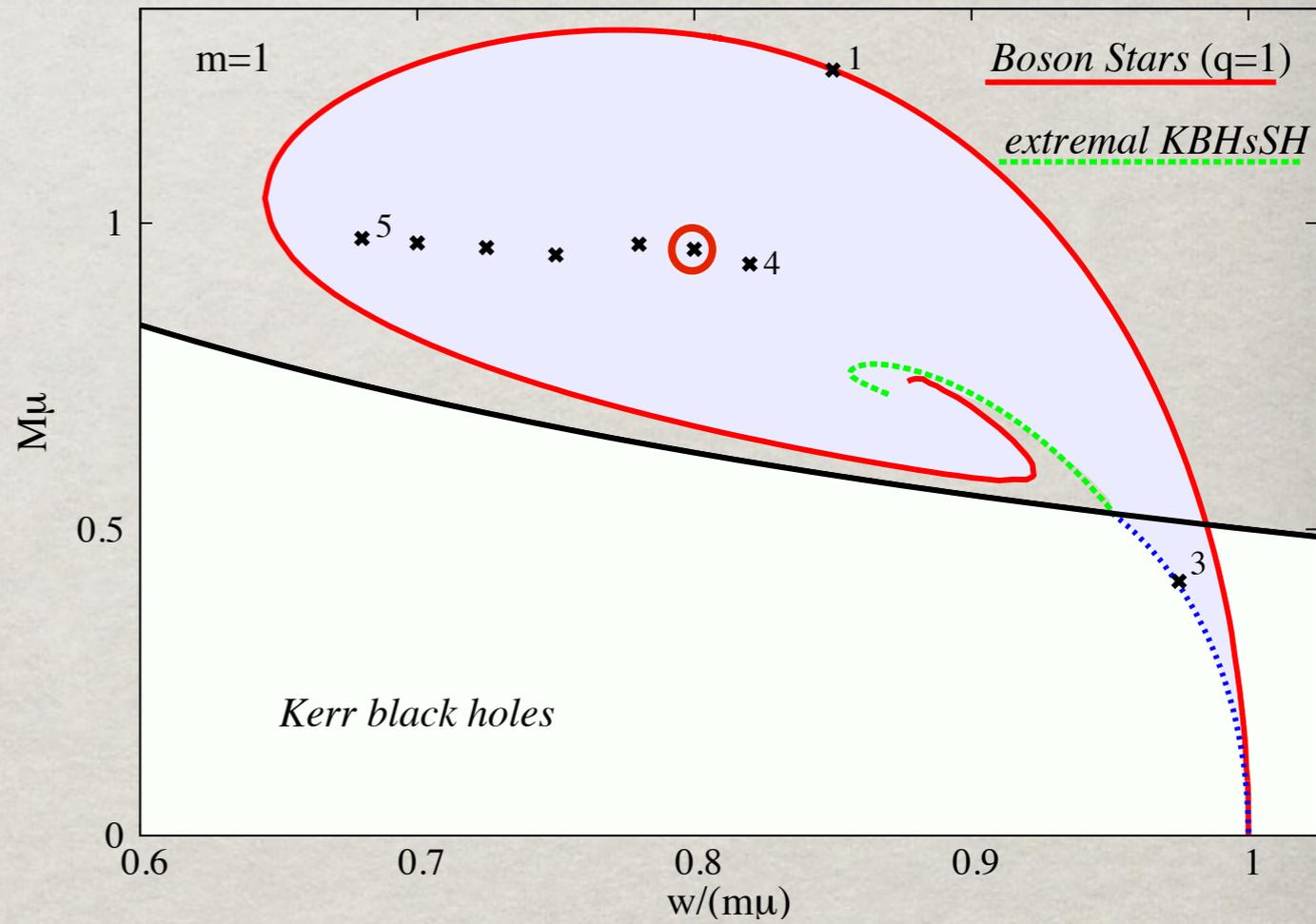
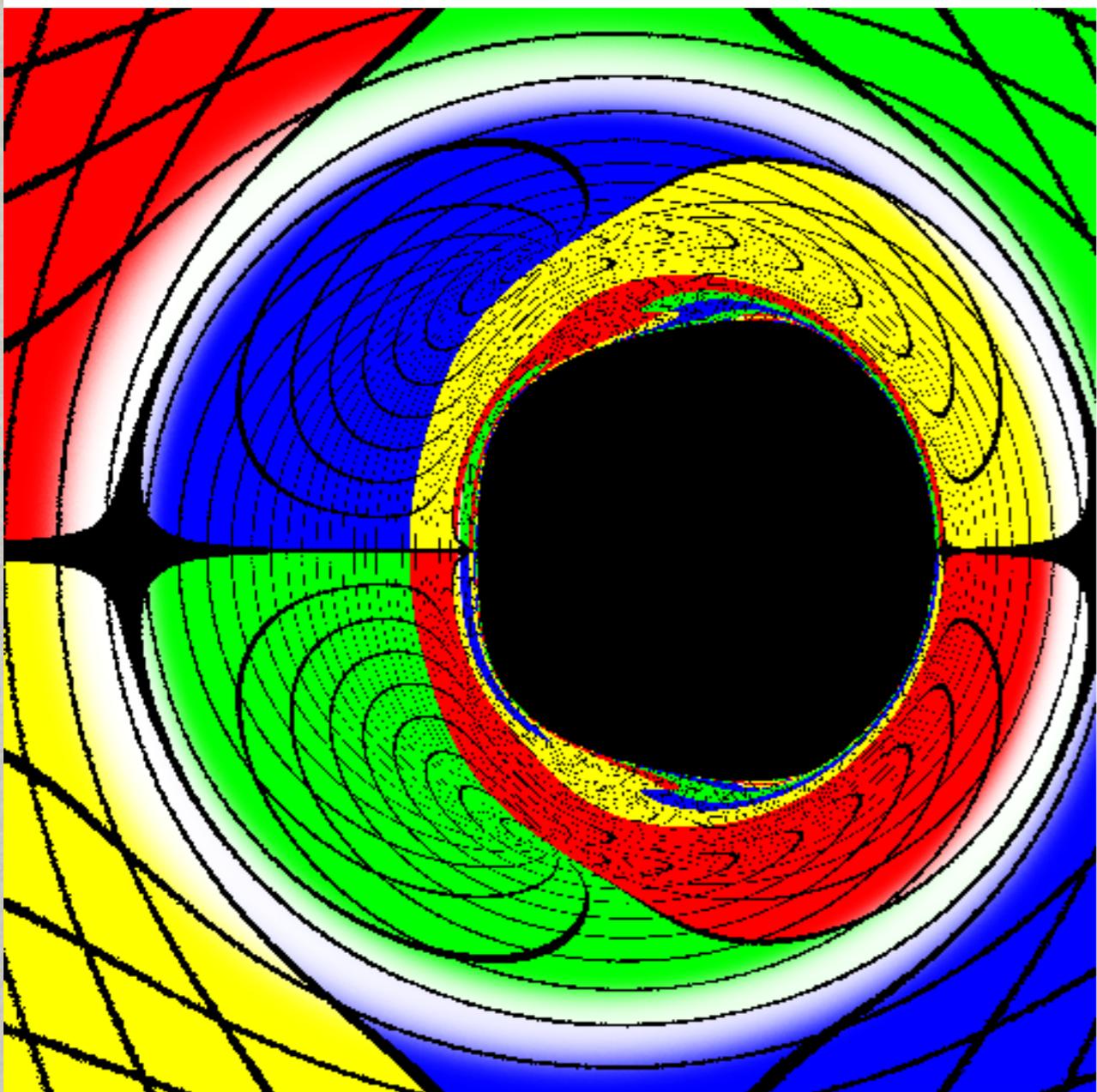
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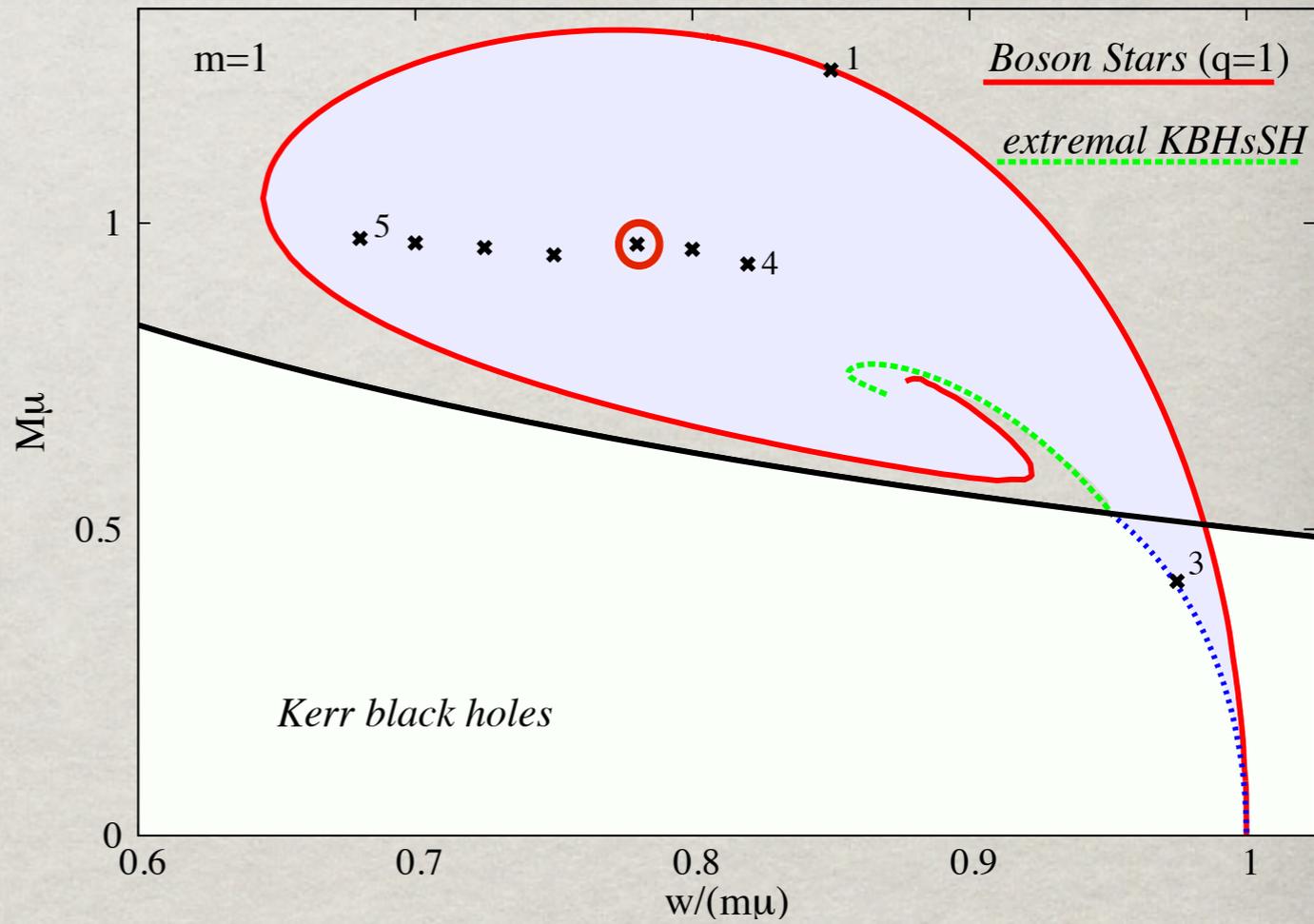
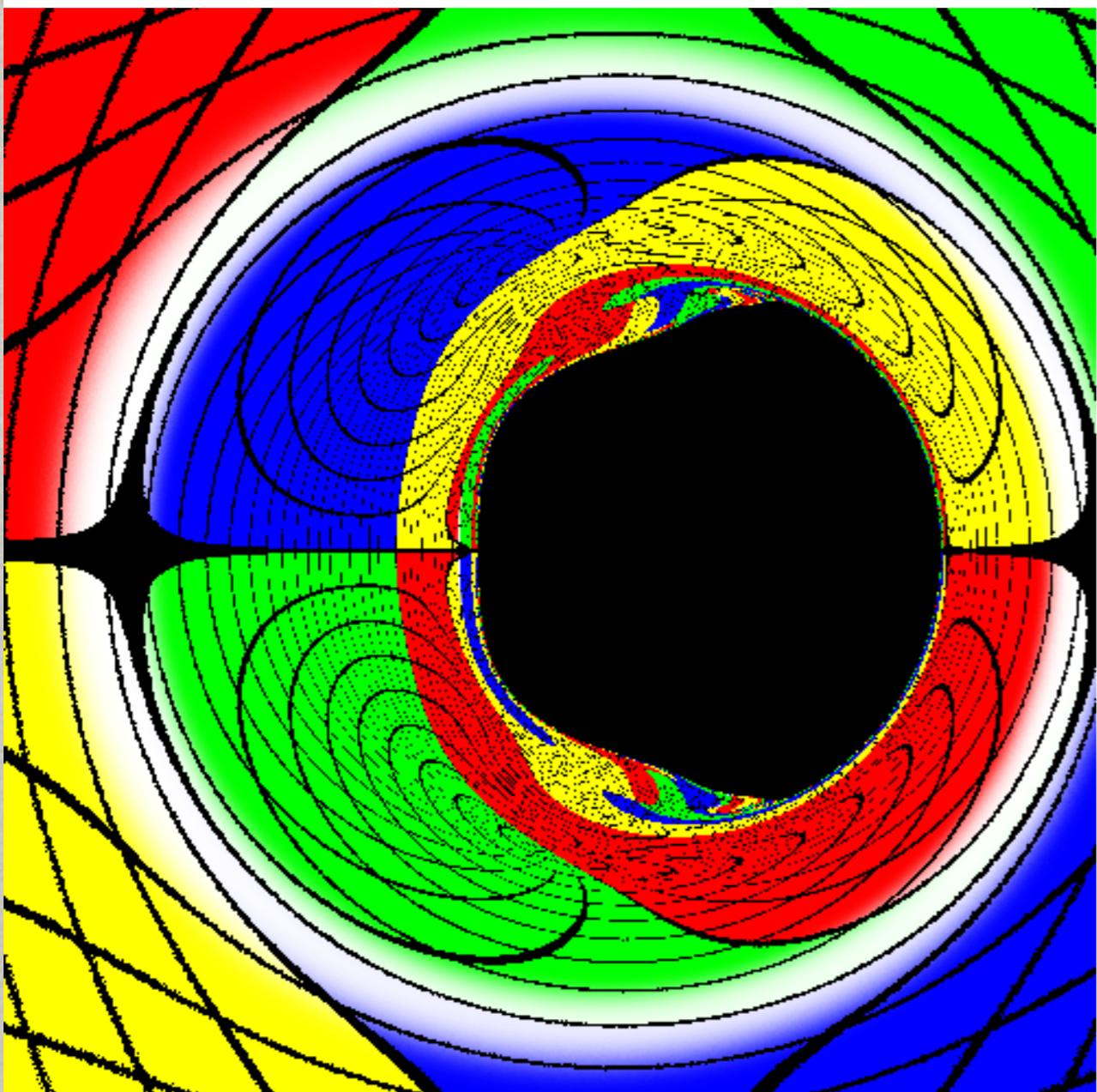
In a toy model it is a hairy black hole of this sort:

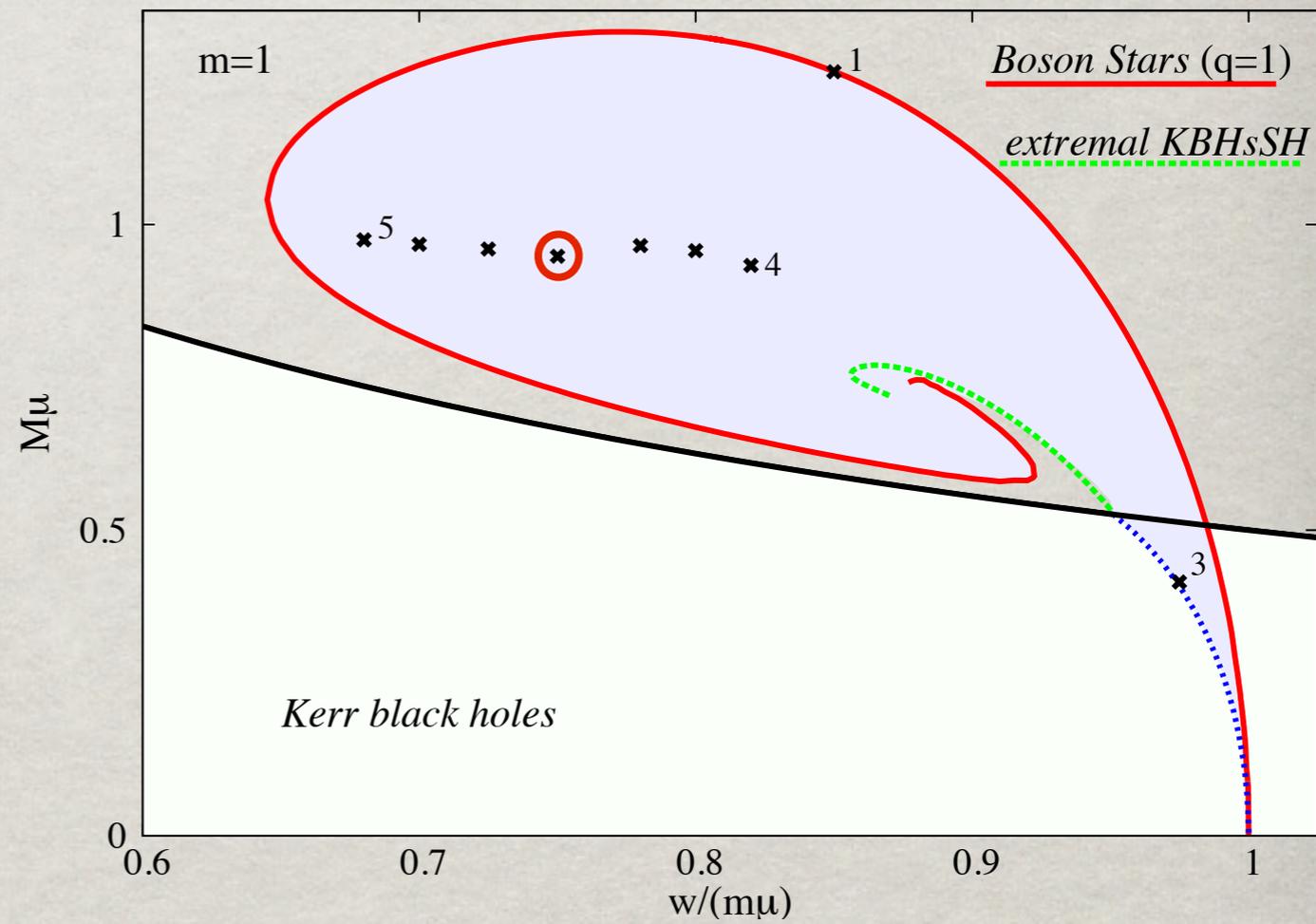
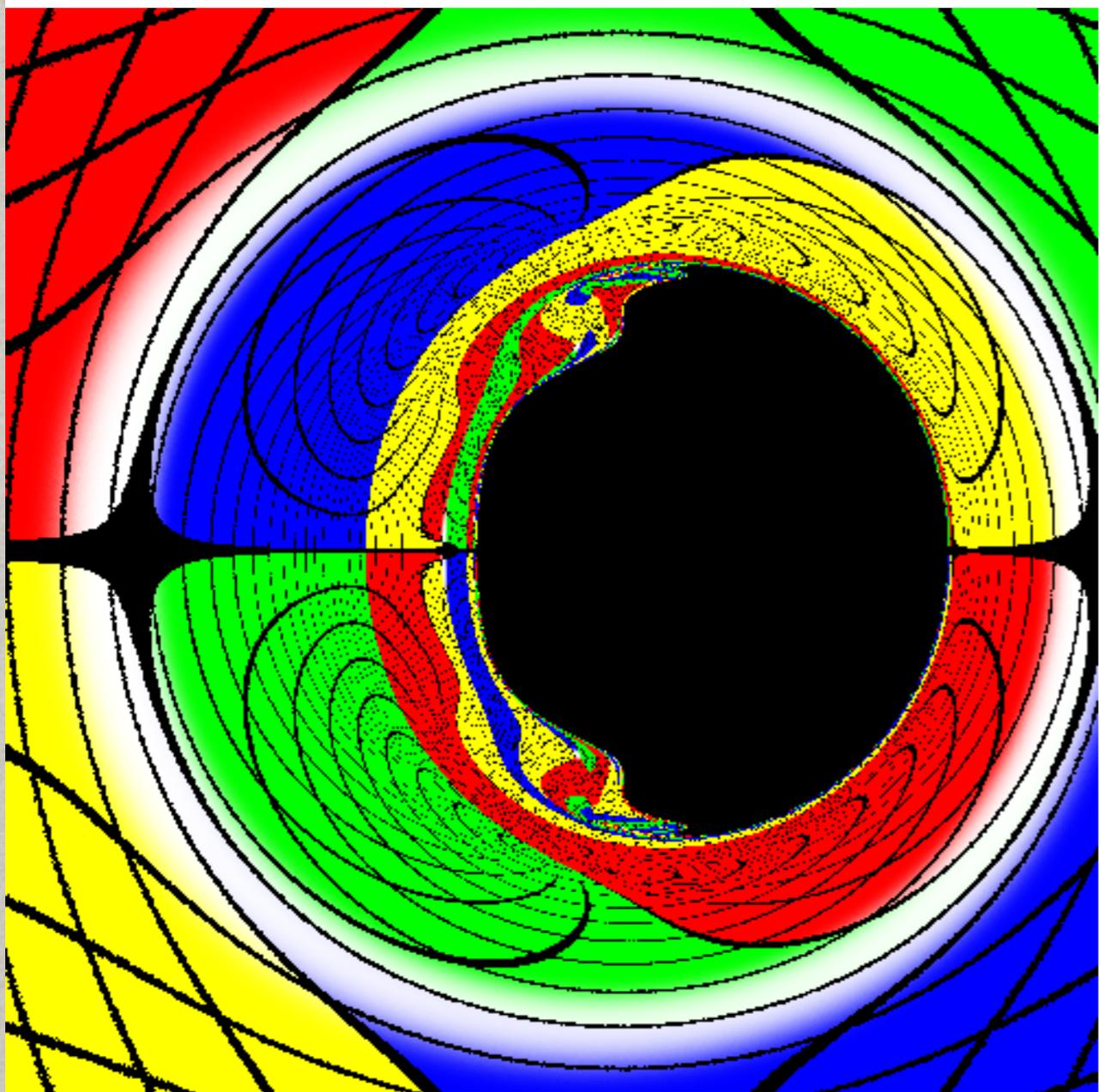
Sanchis-Gual, Degollado, Moreno, Font, C.H.,
PRL 116 (2016)141101

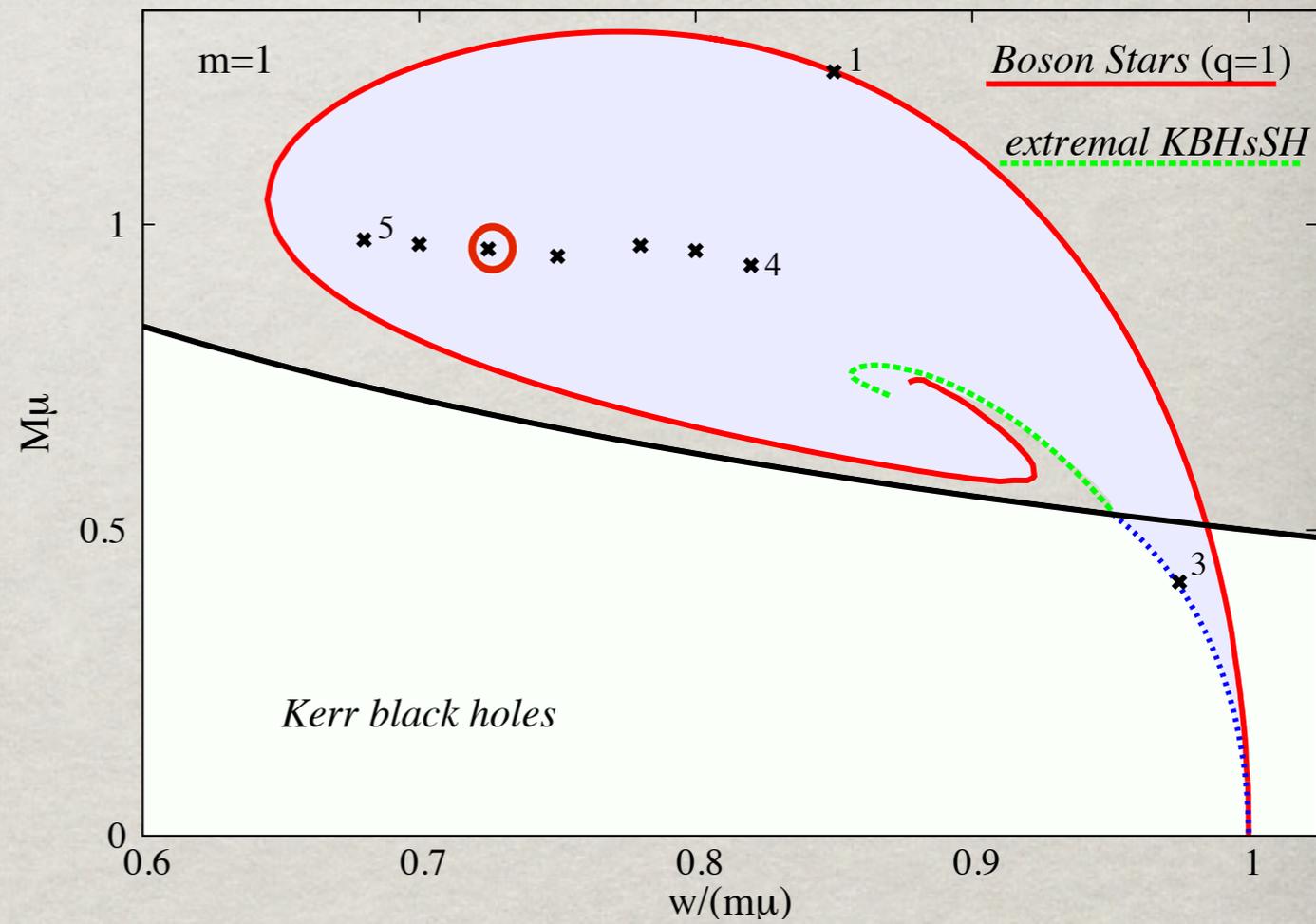
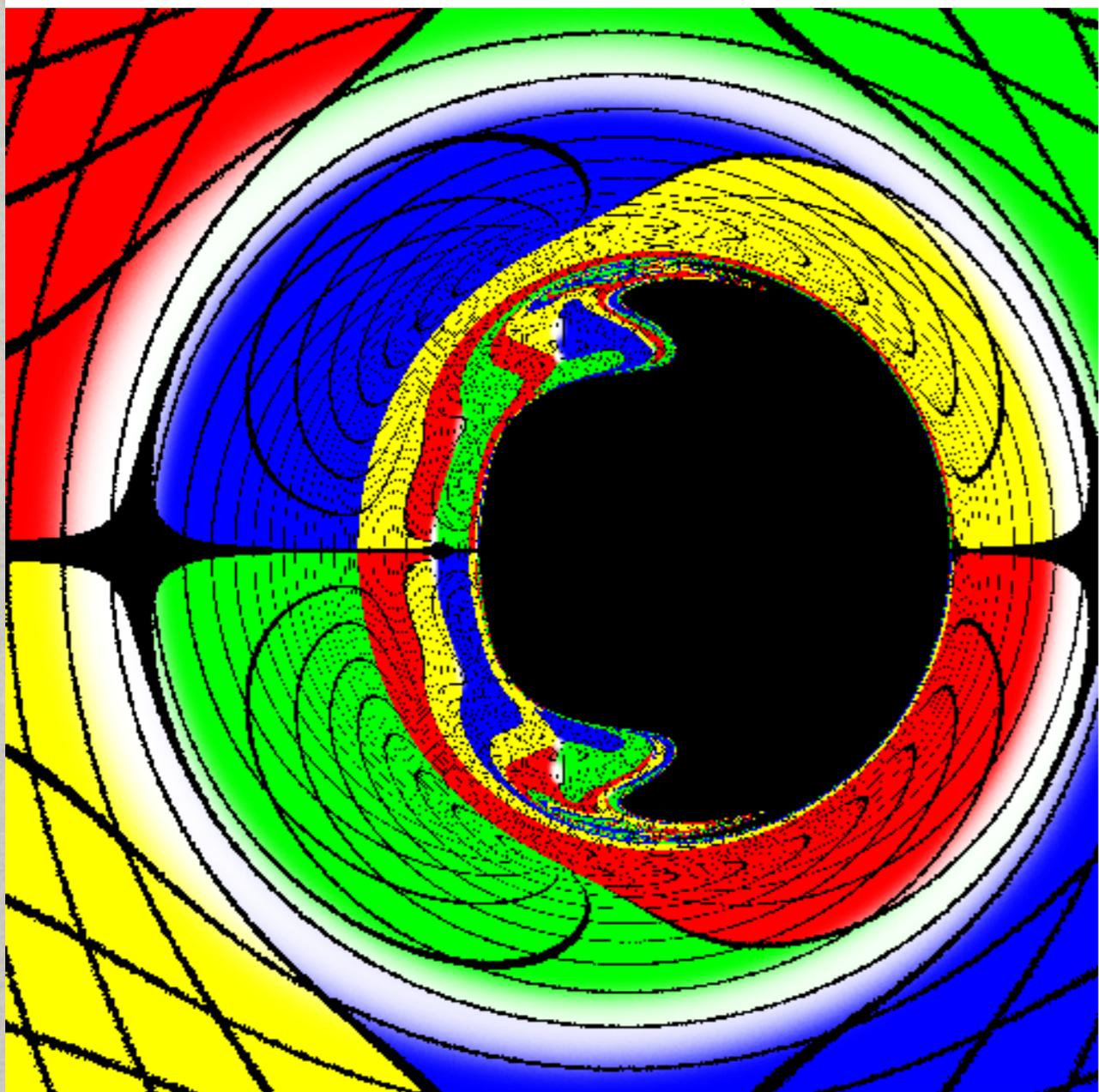
More non-Kerr-like hairy black holes

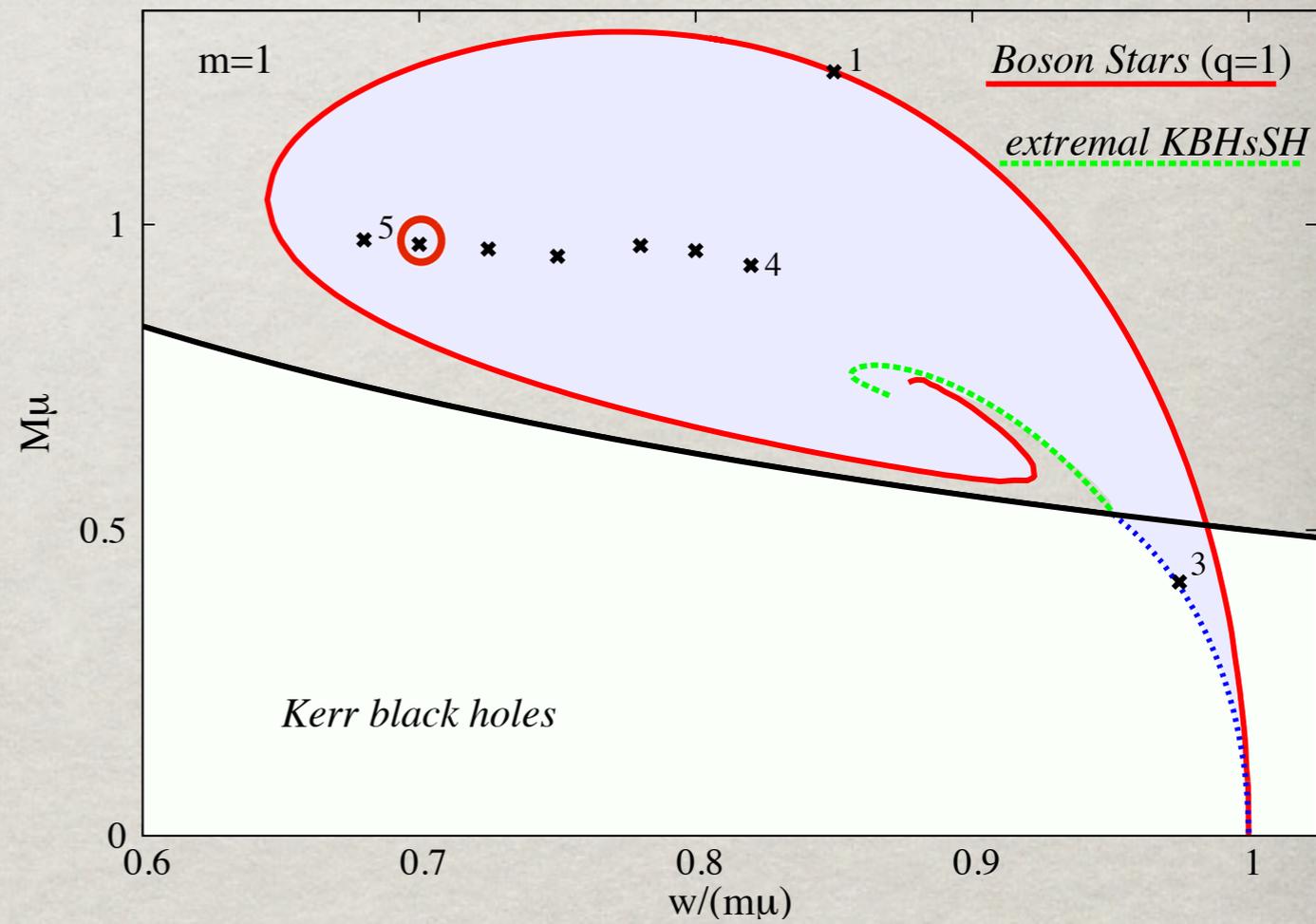
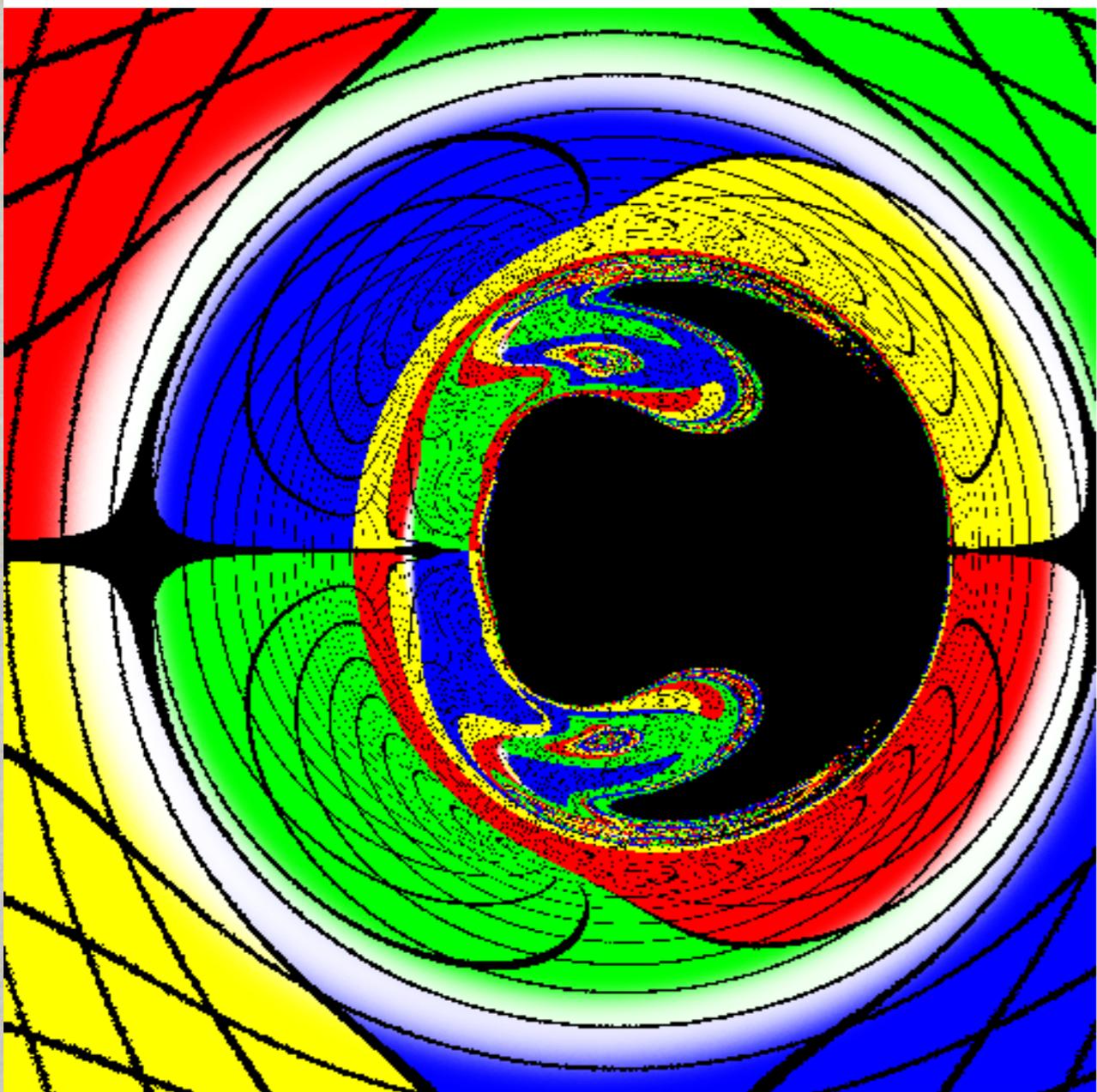


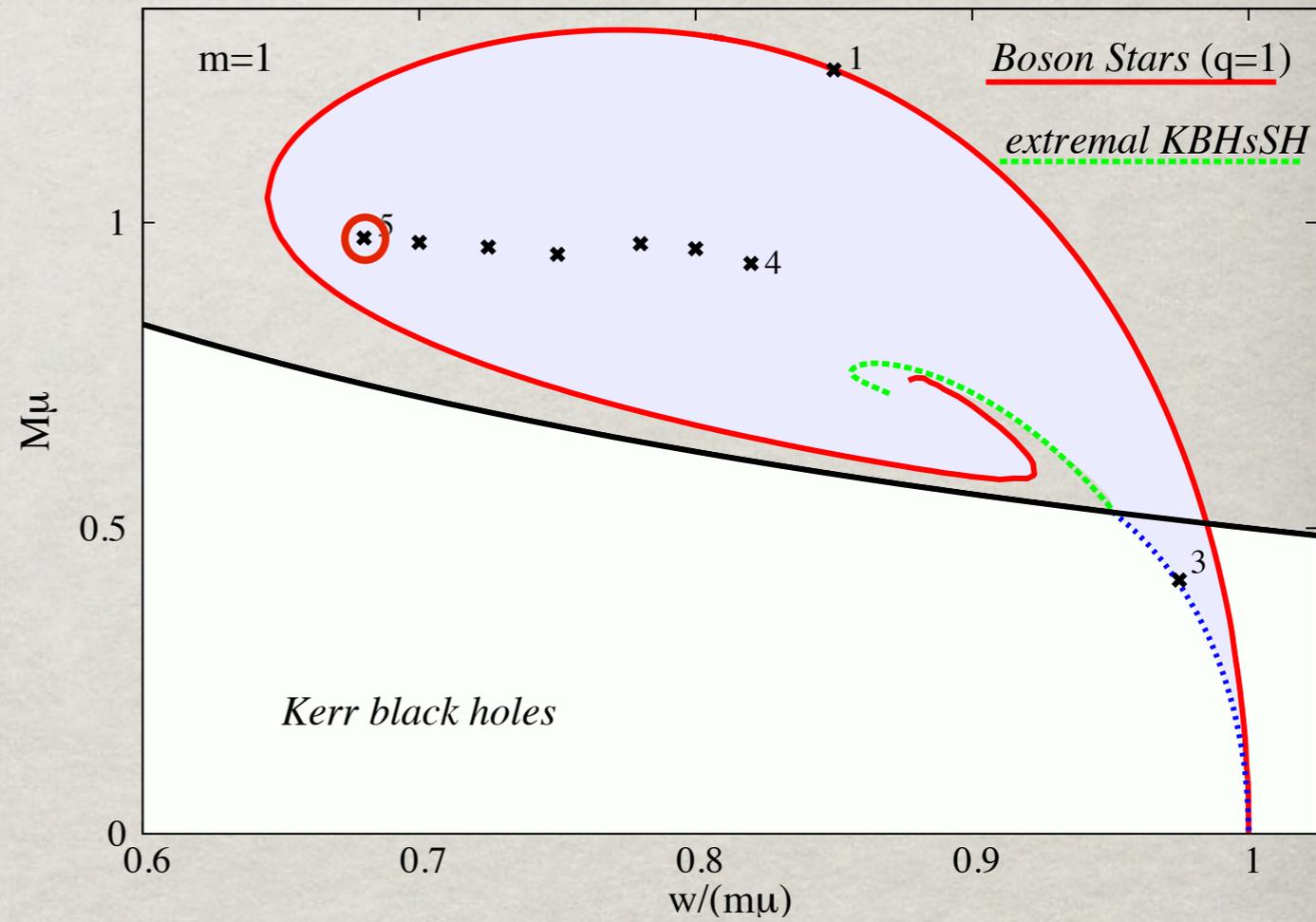
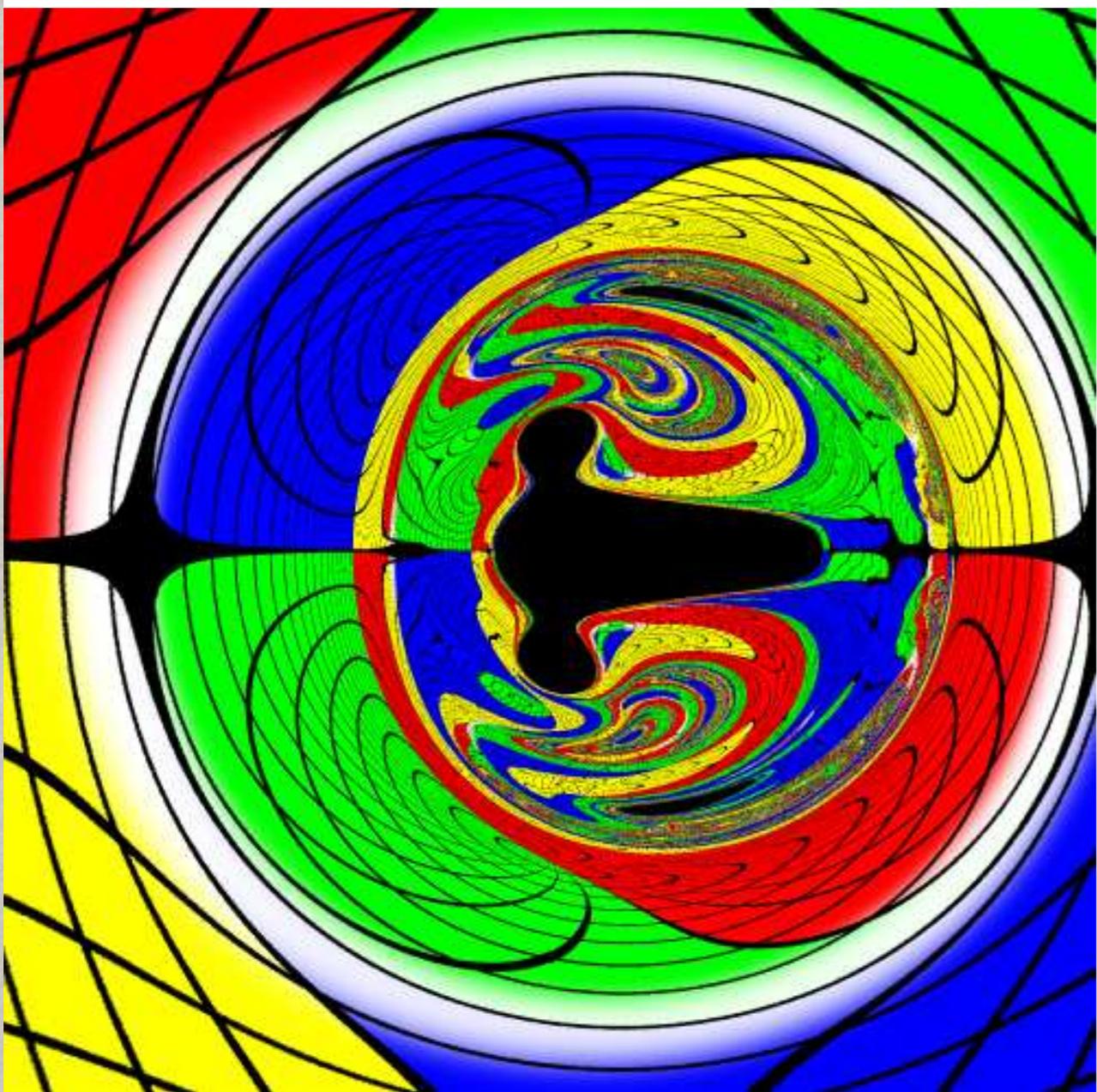




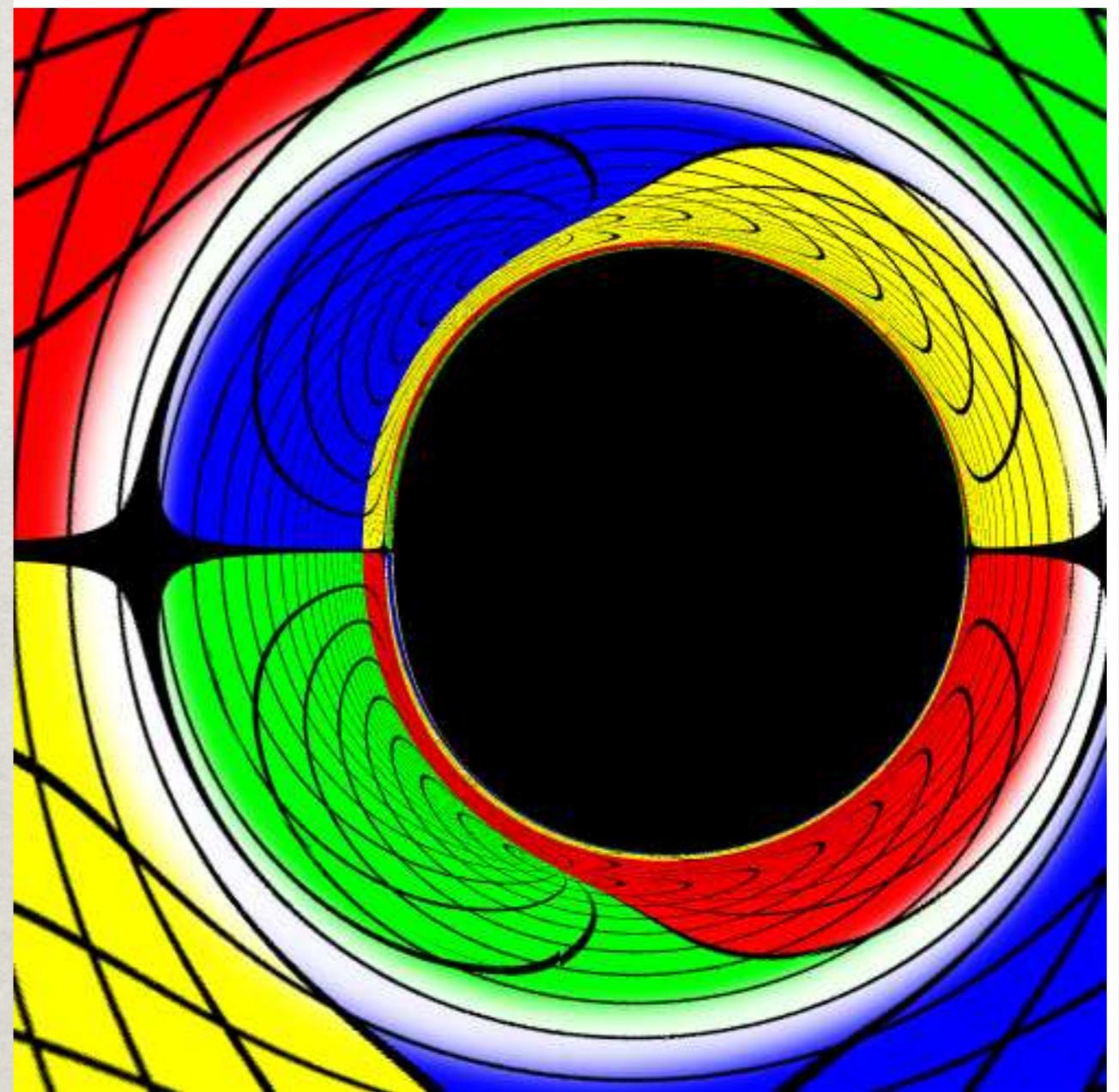
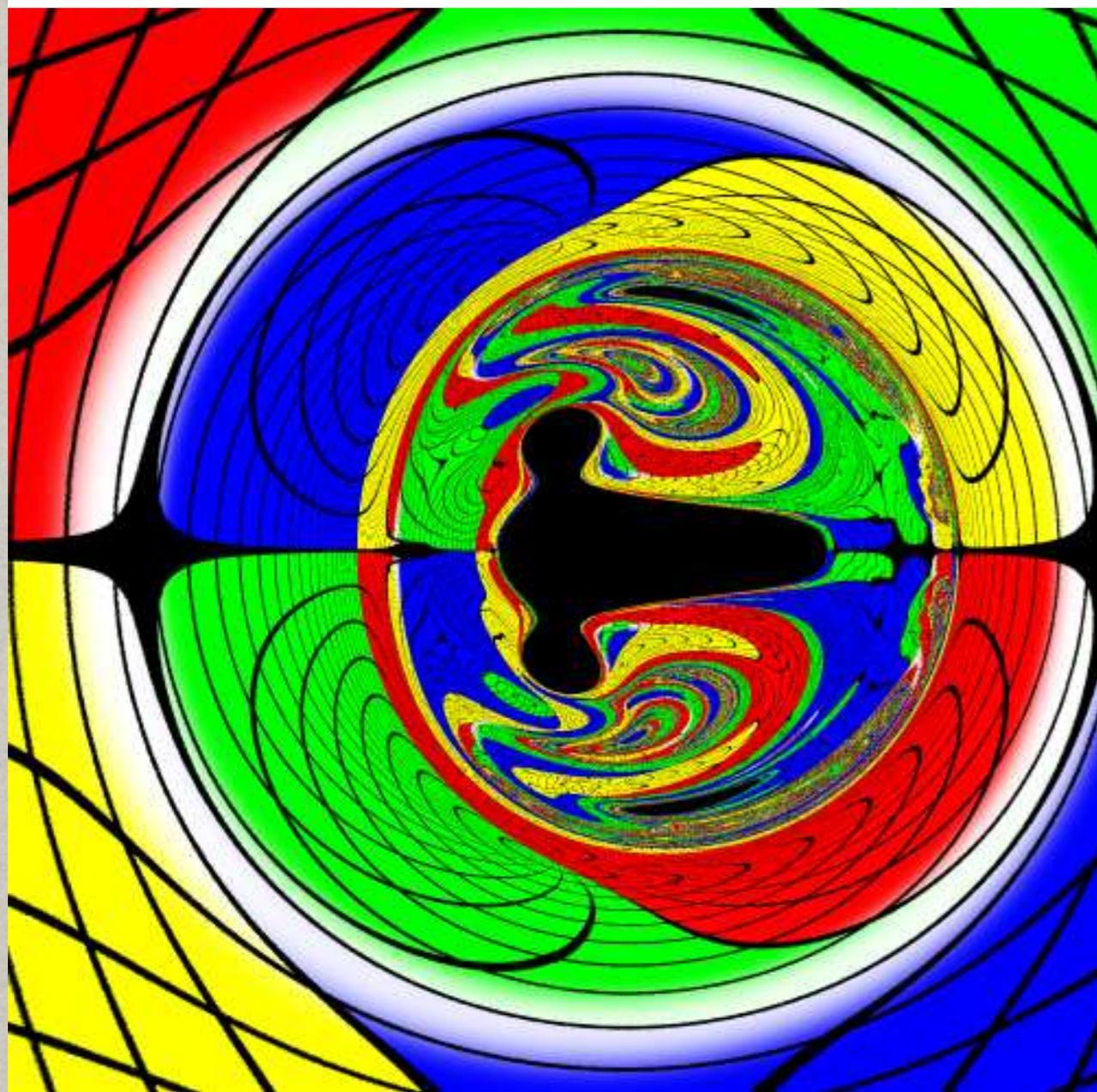








A very non-Kerr-like hairy black hole



Qualitatively new feature:
multiple shadows of a single black hole